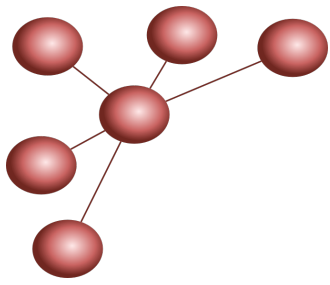


DUBii 2021

# **Introduction to Network Science**

## **Introduction to Network Biology**

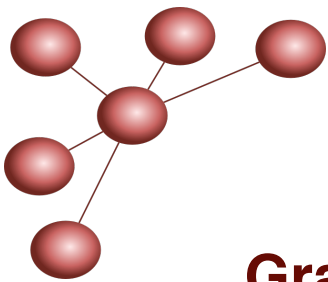
Anaïs Baudot [anais.baudot@univ-amu.fr](mailto:anais.baudot@univ-amu.fr)



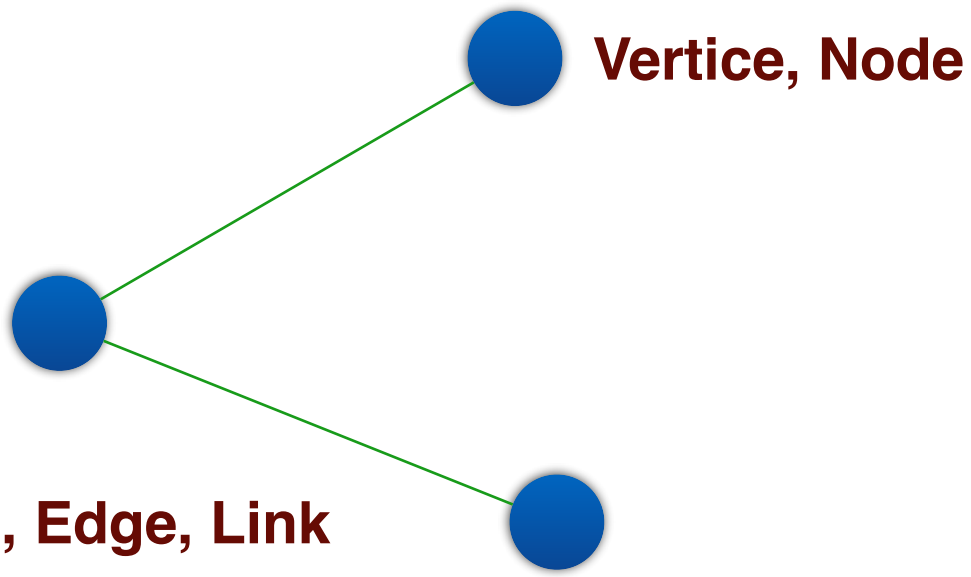
# Network Science

- **Start 21th century**
- **Roots on graph theory**
- **In the context of data production and computer sciences**
- **closely linked to the study of complex systems**

# Definition



**Graph, Network, Web**

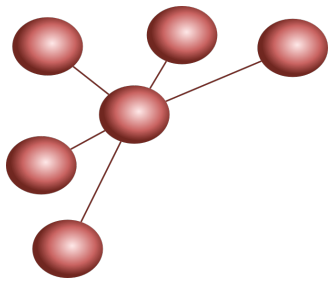


**Vertice, Node**

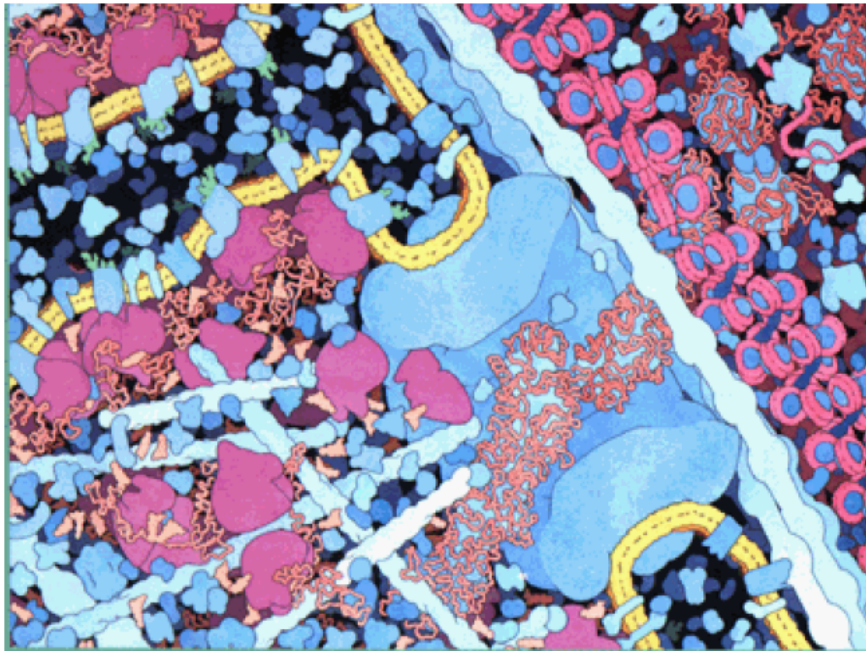
**Interaction, Edge, Link**

$$G = \{V, E\}$$

**Topology, Motifs ...**



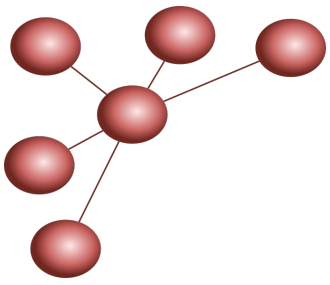
**Macromolecules do not act isolated, but interact with each other to perform their functions**



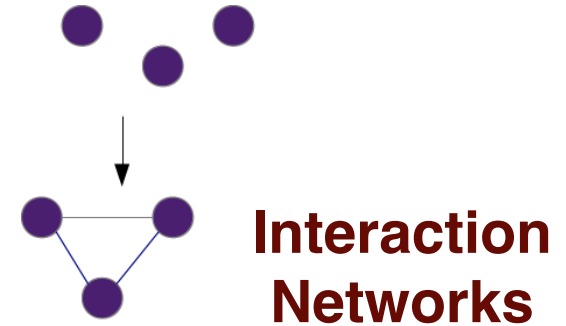
**Molecular interactions:**  
**Protein-Protein**  
**Protein-DNA**  
**Protein-RNA**  
**Protein-Lipid**  
...

**Transient, stable, obligatory ...**

# Systems Biology because living organisms are complex systems



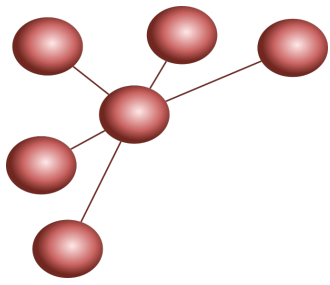
**Systems component : genes/proteins**



**Emerging properties : phenotypes**

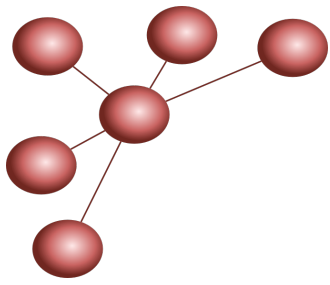


- **Global/collective behaviour cannot be deduced from the knowledge on the components**
- **Phenotype does not emerge from isolated biological molecules but from their interactions**



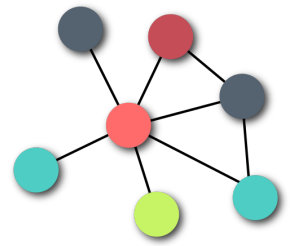
# Part 1: Building Biological Networks

- From literature, knowledge, curation
- From large-scale interaction experiments
- From inference from large-scale omics data



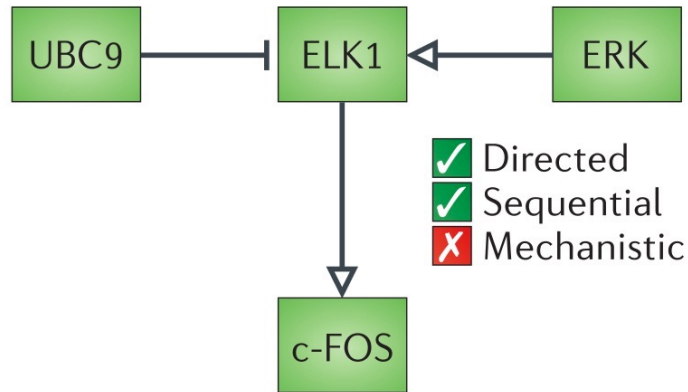
# Part 1: Building Biological Networks

- **From literature, knowledge, curation**
- From large-scale interaction experiments
- From inference from large-scale omics data

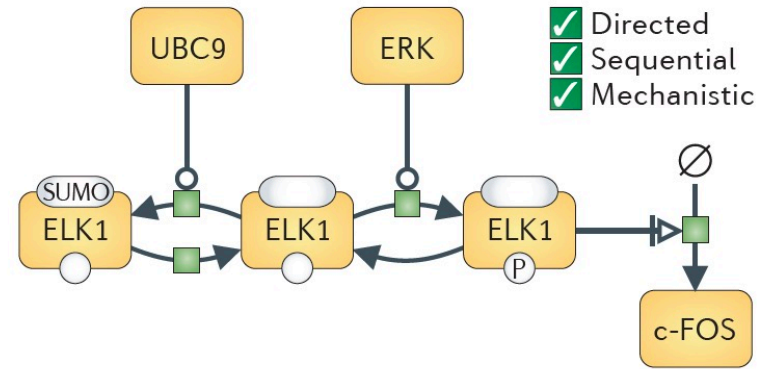


# Building biological networks from literature, knowledge, curation

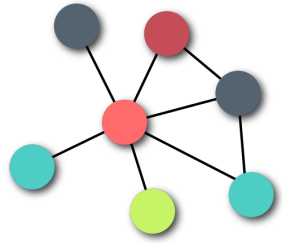
## b Activity flows



## c Process descriptions

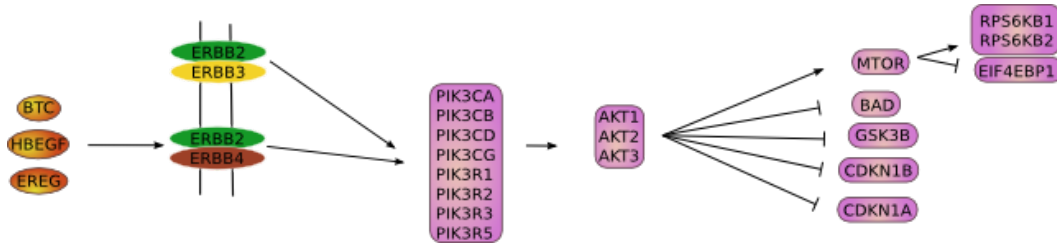




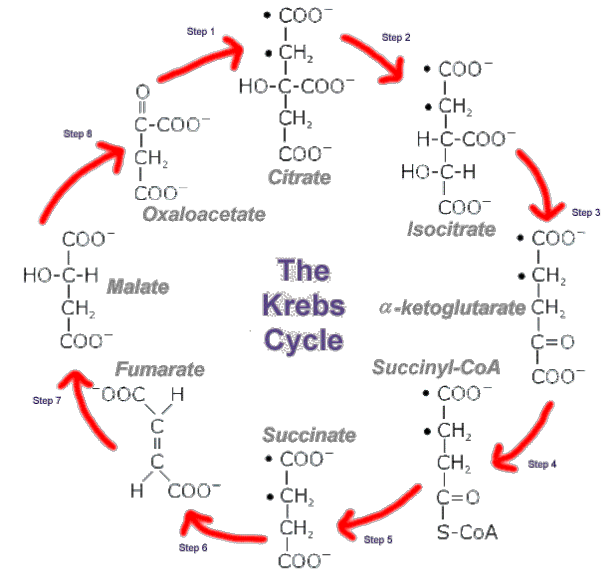


# Activity flow / Gene Regulatory Networks / Influence Graphs

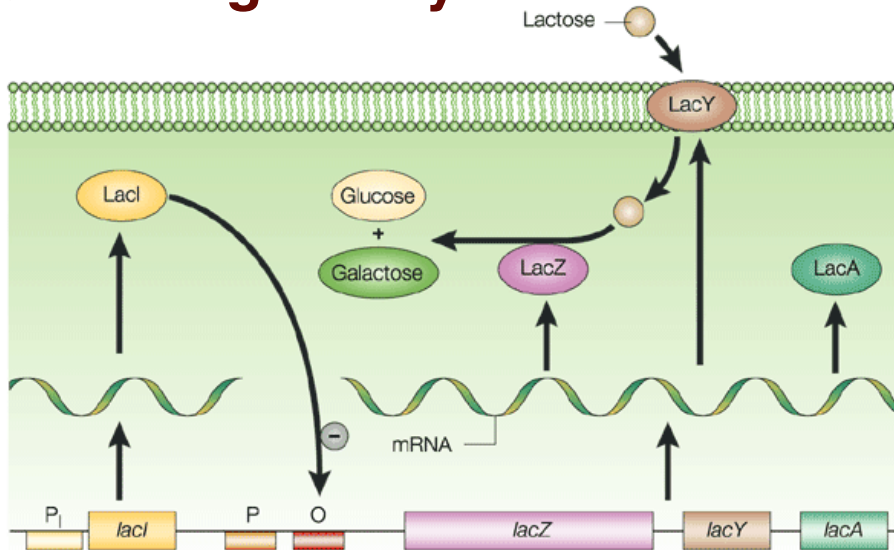
## Signalling networks



## Metabolic Cycle

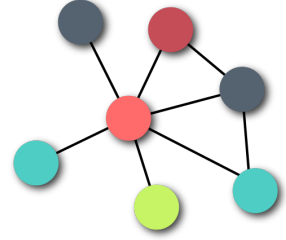


## Gene Regulatory networks



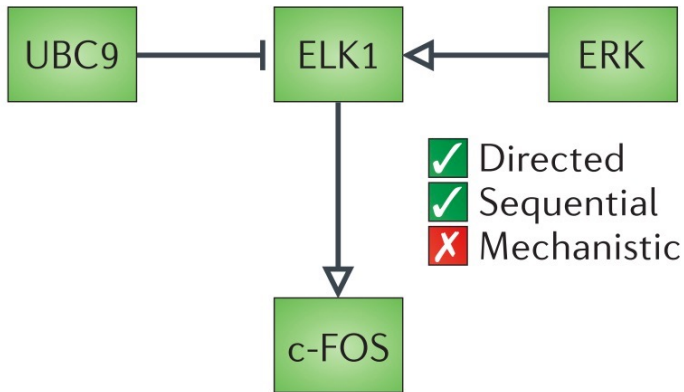
Nature Reviews | Genetics

2 types of nodes : enzymes & substrates, reaction directional or bidirectional

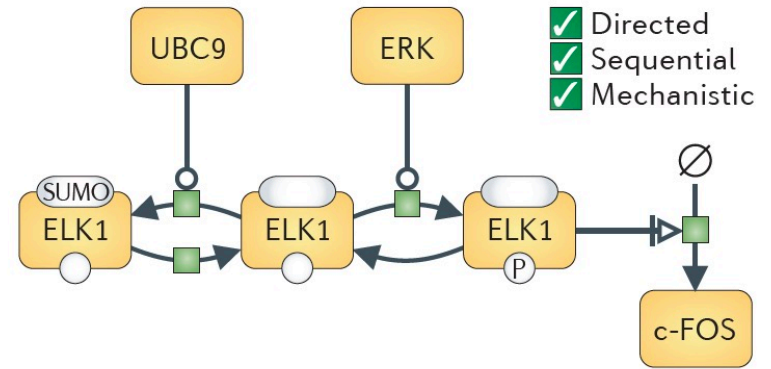


# Building biological networks from literature, knowledge, curation

## b Activity flows



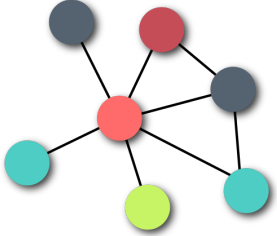
## c Process descriptions



=> pathway databases

=> mathematical modelling





# pathway databases: Kegg



KEGG  Search Help

» Japanese

**KEGG Home**  
 Release notes  
 Current statistics

**KEGG Database**  
 KEGG overview  
 Searching KEGG  
 KEGG mapping  
 Color codes

**KEGG Objects**  
 Pathway maps  
 Brite hierarchies  
 KEGG DB links

**KEGG Software**  
 KEGG API  
 KGML

KEGG FTP  
 Subscription  
 Background info

GenomeNet  
 DBGET/LinkDB  
 Feedback  
 Copyright request

Kanehisa Labs

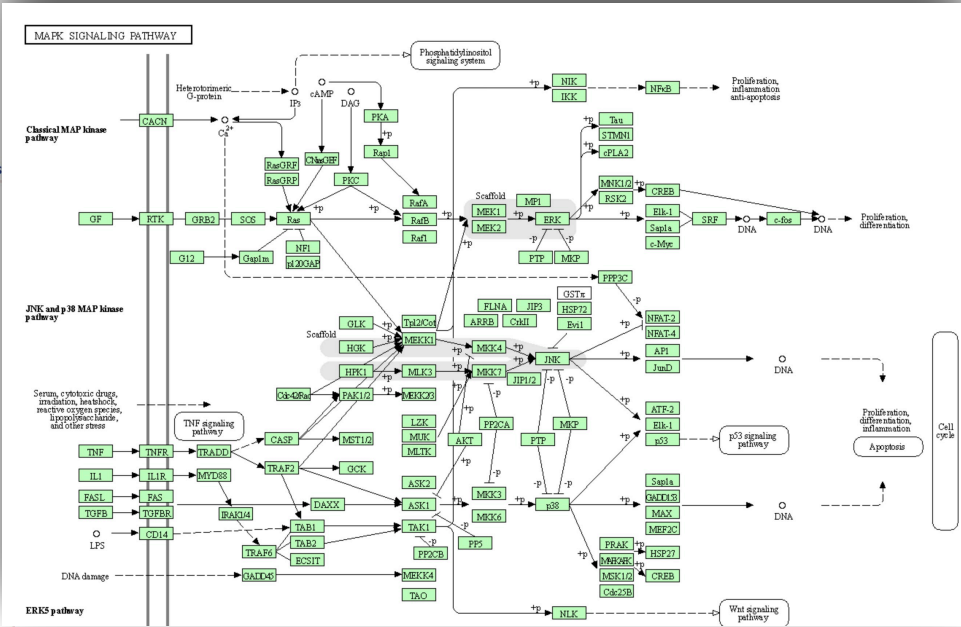
## KEGG: Kyoto Encyclopedia of Genes and Genomes

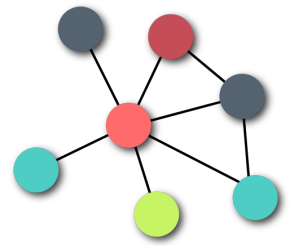
KEGG is a database resource for understanding high-level functions and utilities of the biological system, such as the cell, the organism and the ecosystem, from molecular-level information, especially large-scale molecular datasets generated by genome sequencing and other high-throughput experimental technologies. See [Release notes](#) (January 1, 2021) for new and updated features.

**New article** [KEGG: integrating viruses and cellular organisms](#)

- **Main entry point to the KEGG web service**  
**KEGG2**      KEGG Table of Contents    [Update notes | Release history]
- **Data-oriented entry points**
  - KEGG PATHWAY**    KEGG pathway maps
  - KEGG BRITE**        BRITE hierarchies and tables
  - KEGG MODULE**    KEGG modules
  - KEGG ORTHOLOGY** KO functional orthologs    [Annotation]
  - KEGG GENOME**    Genomes    [Pathogen | Virus | Plant]
  - KEGG GENES**      Genes and proteins    [SeqData]
  - KEGG COMPOUND** Small molecules
  - KEGG GLYCAN**     Glycans
  - KEGG REACTION**    Biochemical reactions    [RModule]
  - KEGG ENZYME**    Enzyme nomenclature
  - KEGG NETWORK**    Disease-related network variations
  - KEGG DISEASE**    Human diseases
  - KEGG DRUG**        Drugs    [New drug approvals]
  - KEGG MEDICUS**    Health information resource    [Drug labels search]
- **Organism-specific entry points**  
**KEGG Organisms**    Enter org code(s)      hsa    hsa eco
- **Analysis tools**
  - KEGG Mapper**      KEGG PATHWAY/BRITE/MODULE mapping tools
  - BlastKOALA**        BLAST-based KO annotation and KEGG mapping
  - GhostKOALA**        GHOSTX-based KO annotation and KEGG mapping
  - KofamKOALA**        HMM profile-based KO annotation and KEGG mapping
  - BLAST/FASTA**        Sequence similarity search
  - SIMCOMP**            Chemical structure similarity search

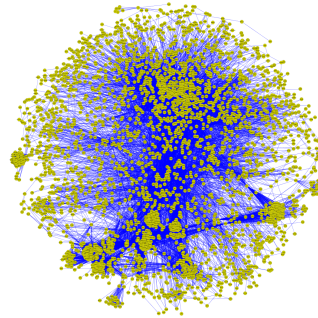
Pathway  
 Brite  
 Brite table  
 Module  
 Network  
 KO (Function)  
 Organism  
 Virus  
 Compound  
 Disease (ICD)  
 Drug (ATC)  
 Drug (Target)





# pathway databases

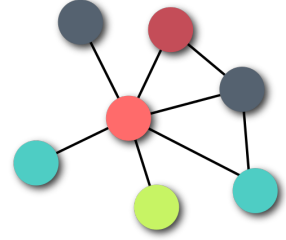
## Pathways



~250 000 edges

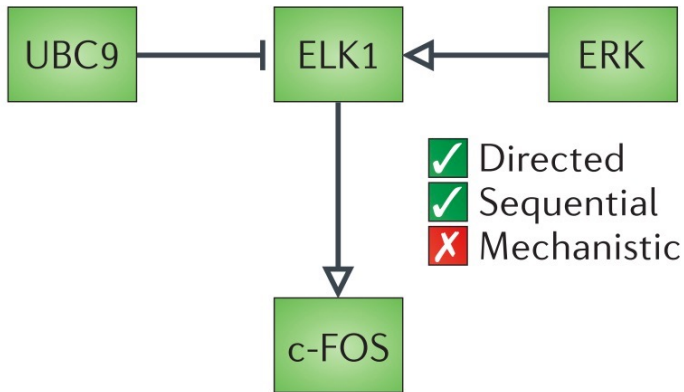
---

Curated  
networks

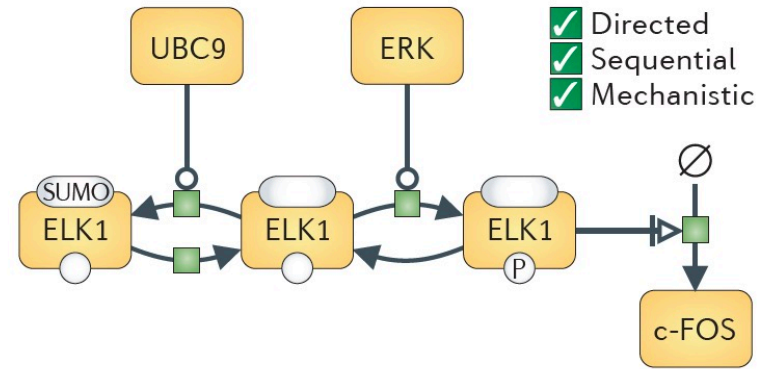


# Building biological networks from literature, knowledge, curation

## b Activity flows

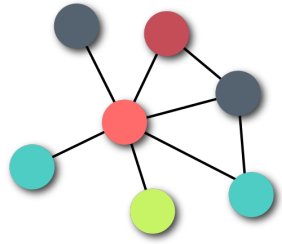


## c Process descriptions

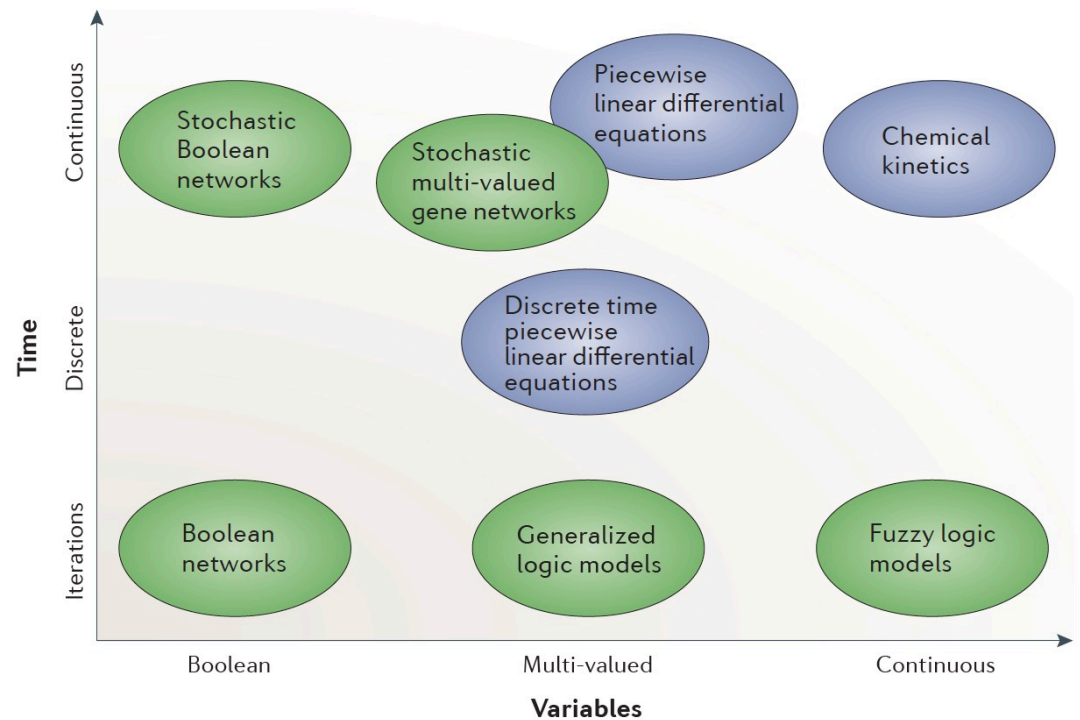
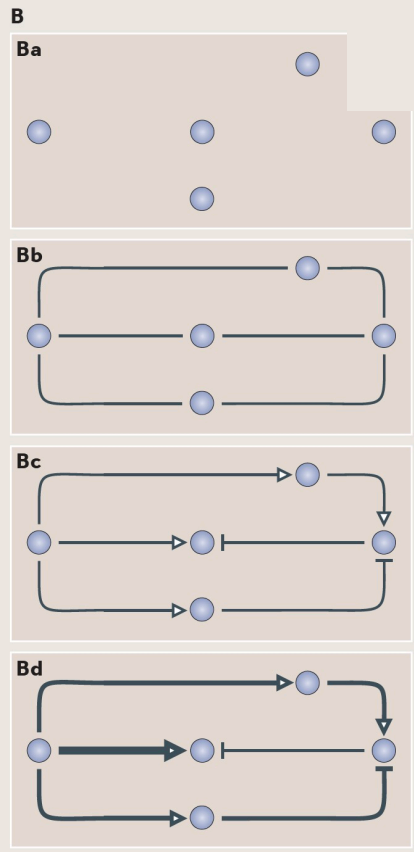
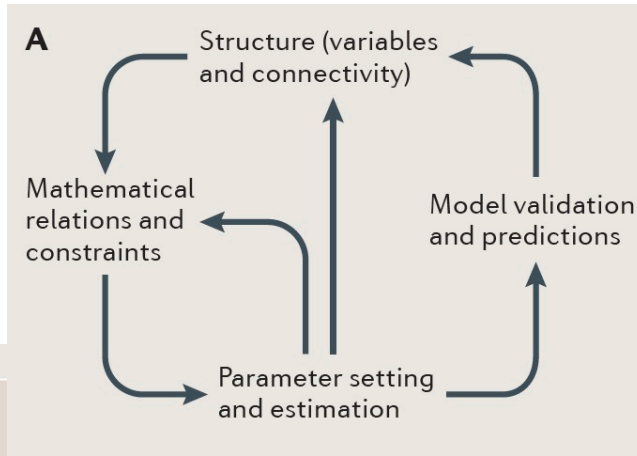


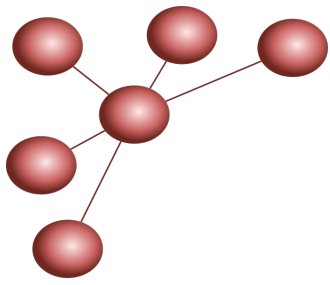
=> pathway databases

=> mathematical modelling



# Building mathematical models of biological processes

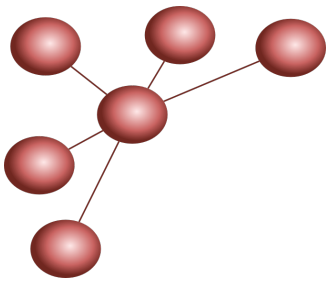




# Part 1: Building Biological Networks

- From literature, knowledge, curation
- **From large-scale interaction experiments**
- From inference from large-scale omics data



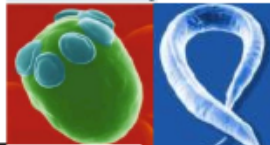
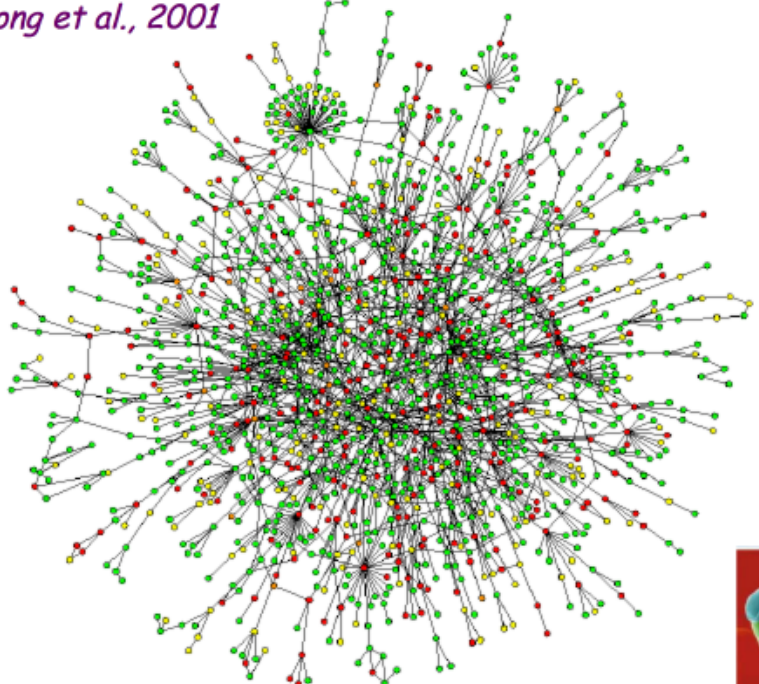


# Experimental interaction screenings

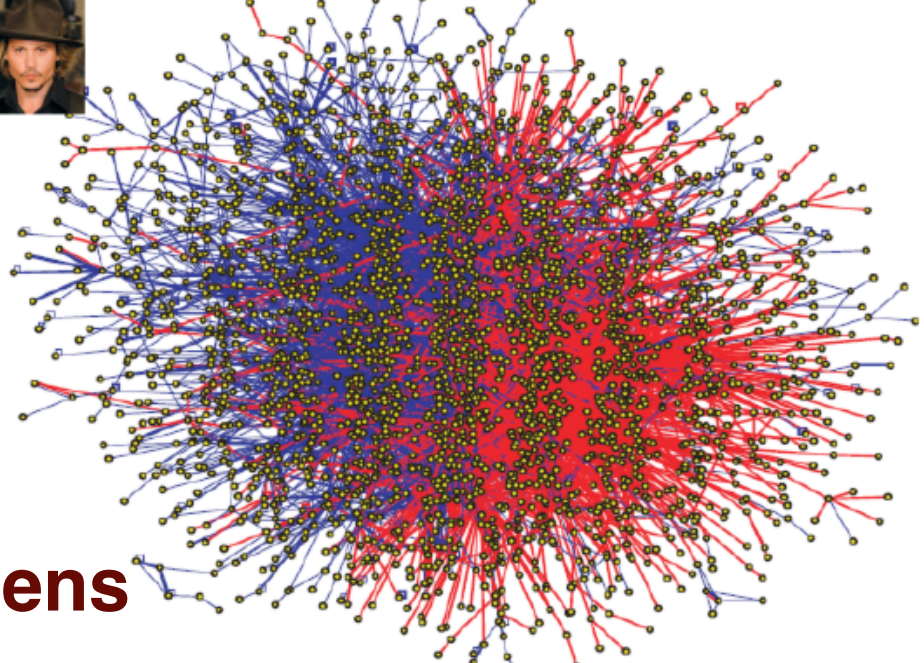
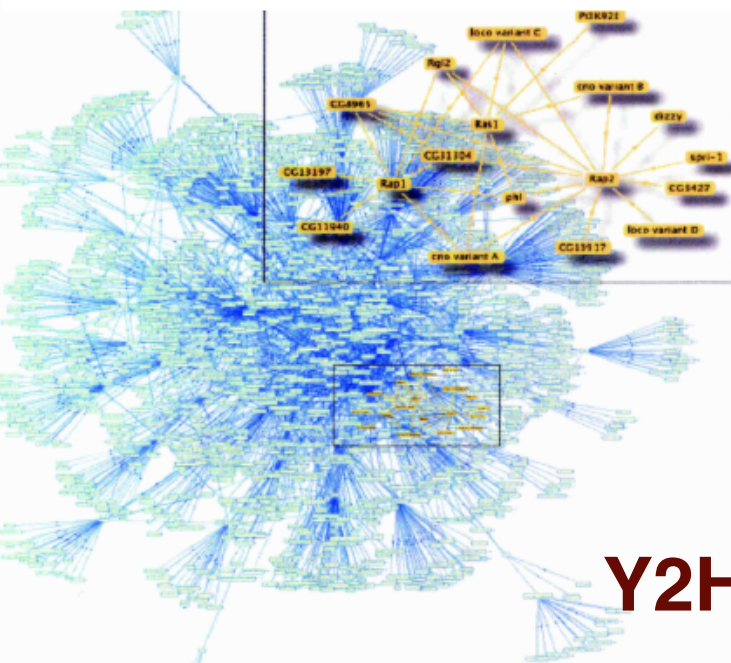
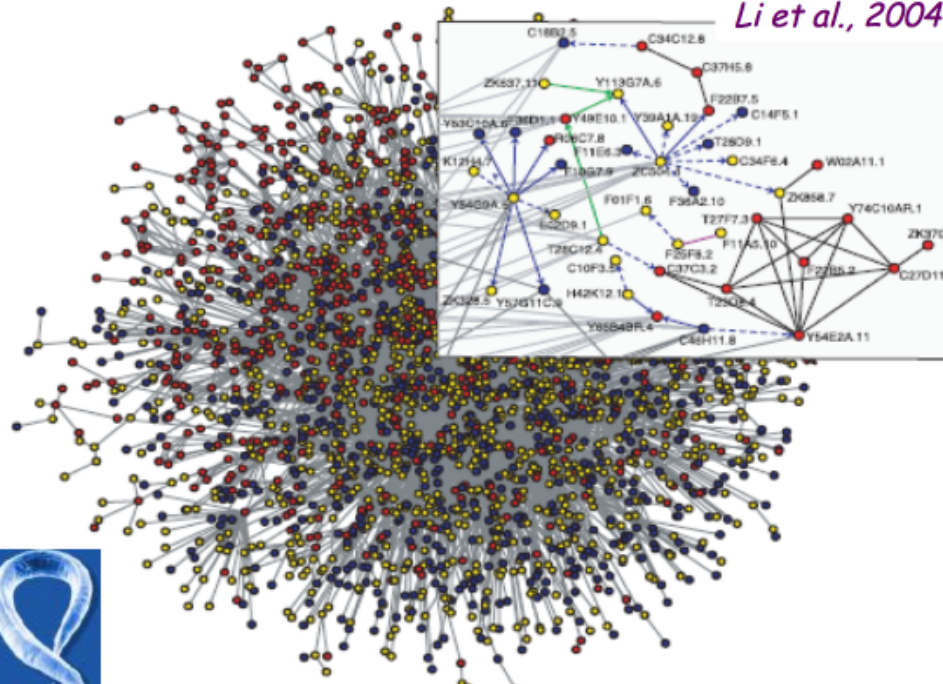
- Protein-protein interactions
- Protein-DNA interactions
- Protein-RNA interactions
- ...

=> Small-scale / Large-scale

Jeong et al., 2001



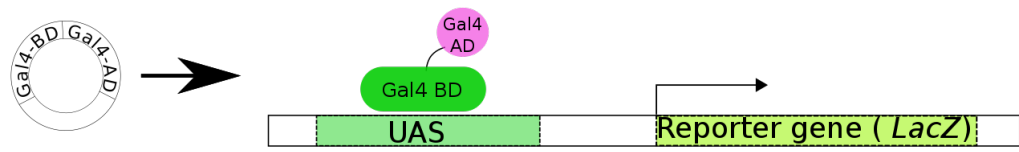
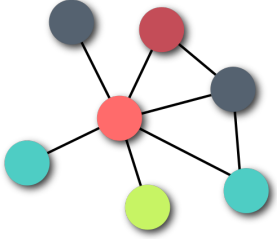
Li et al., 2004



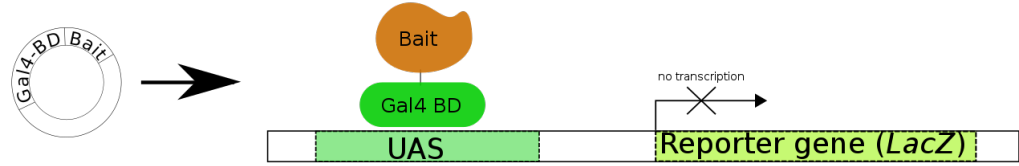
# Y2H screens

Formstecher et al., 2005

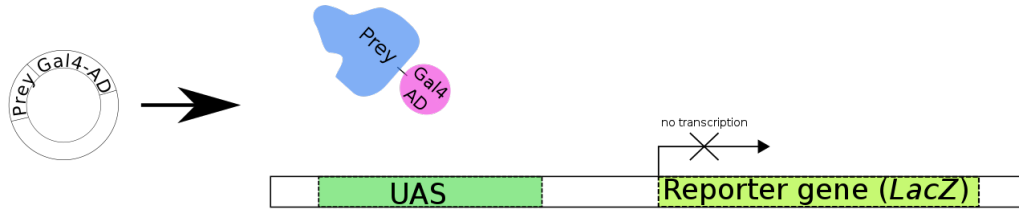
Rual et al., 2005



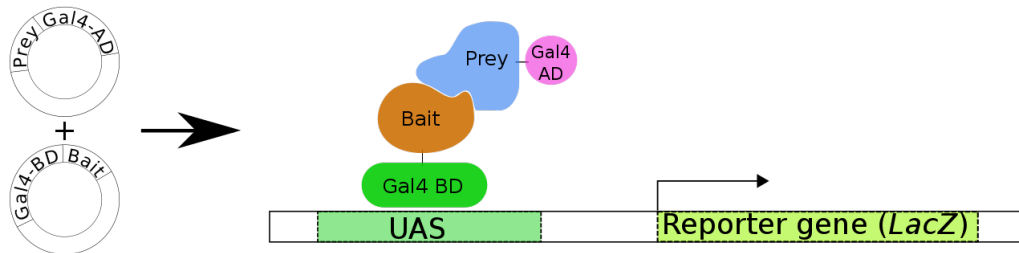
A. Regular transcription of the reporter gene



B. One fusion protein only (Gal4-BD + Bait) - no transcription

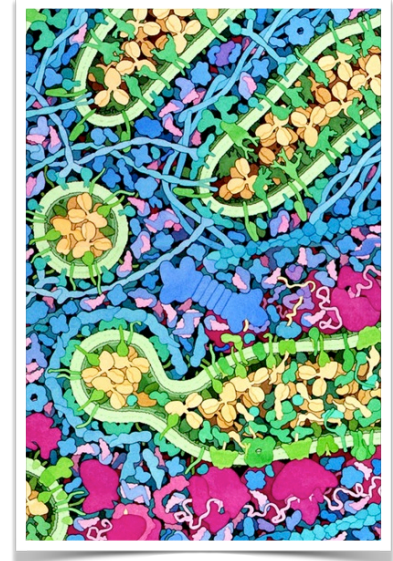
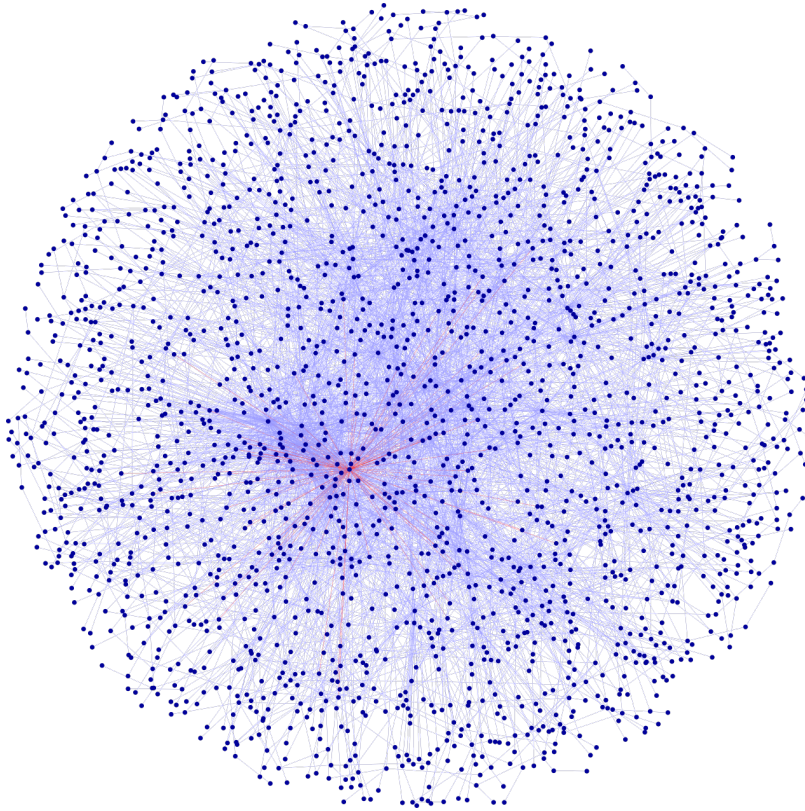
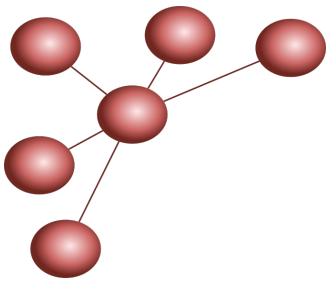


C. One fusion protein only (Gal4-AD + Prey) - no transcription



D. Two fusion proteins with interacting Bait and Prey

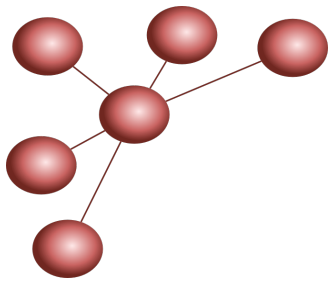
# Interactomes: protein-protein interactions



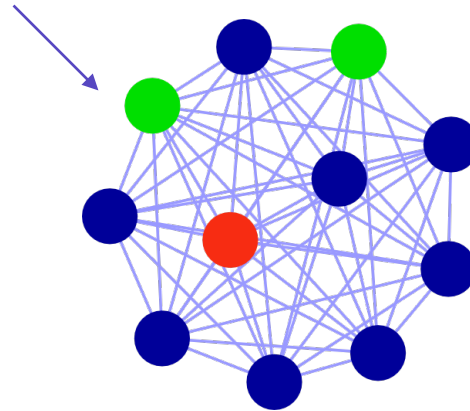
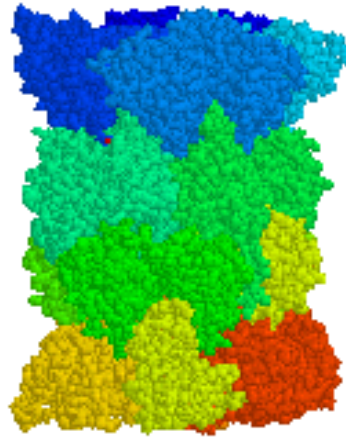
**Set of detected protein-protein interactions**

Physical interactions, but  
physiological interactions ?

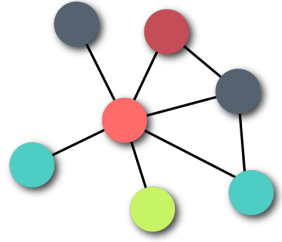
Interactomes are devoid of spatio-  
temporal information



# Interactomes: Pull-Down



**Protein complexes**



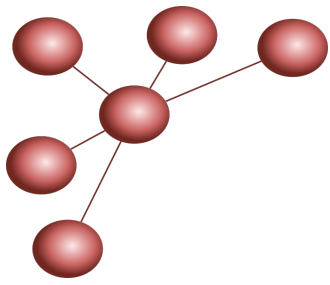
# False-negatives and “sparse networks”

Interaction space (to be discovered)



Interactions discovered by method 1

Interactions discovered by method 2



# Interaction databases

Multi-organisms:

DIP ([dip.doe-mbi.ucla.edu](http://dip.doe-mbi.ucla.edu))

**IntAct** ([www.ebi.ac.uk/intact](http://www.ebi.ac.uk/intact))

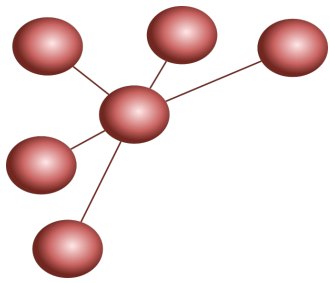
MINT ([mint.bio.uniroma2.it/mint](http://mint.bio.uniroma2.it/mint))

BioGRID ([www.thebiogrid.org](http://www.thebiogrid.org))

BIND ([www.blueprint.org](http://www.blueprint.org))



**International  
Molecular  
Exchange  
Consortium**



# PSICQUIC portal

EMBL-EBI

Services Research Training About us

## PSICQUIC View

BRCA2

Examples: BRCA2\_Q06609,dmc1,10831611

Search

Input Form **Browse** Help

Feedback

[Input Form](#) > [Browse](#)

1,832 binary interactions found for search term **BRCA2**

- |   |  |   |  |
|---|--|---|--|
| <input type="checkbox"/> APID Interactomes      | <input checked="" type="checkbox"/> BAR              | <input checked="" type="checkbox"/> bhf-ucl         | <input type="checkbox"/> BIND                            |
| <input checked="" type="checkbox"/> BindingDB-0 | <input checked="" type="checkbox"/> BioGrid-322      | <input checked="" type="checkbox"/> ChEMBL-0        | <input type="checkbox"/> DIP                             |
| <input type="checkbox"/> DIP-IMEx               | <input type="checkbox"/> DrugBank                    | <input checked="" type="checkbox"/> EBI-GOA-miRNA-0 | <input checked="" type="checkbox"/> EBI-GOA-nonIntAct-65 |
| <input type="checkbox"/> GeneMANIA              | <input checked="" type="checkbox"/> HPIDb-0          | <input checked="" type="checkbox"/> I2D-0           | <input checked="" type="checkbox"/> IMEx-241             |
| <input checked="" type="checkbox"/> InnateDB-0  | <input checked="" type="checkbox"/> InnateDB-All-561 | <input checked="" type="checkbox"/> IntAct-107      | <input type="checkbox"/> Interoprc                       |
| <input type="checkbox"/> iRefIndex              | <input checked="" type="checkbox"/> MatrixDB-12      | <input checked="" type="checkbox"/> MBIInfo-0       | <input checked="" type="checkbox"/> mentha-380           |
| <input checked="" type="checkbox"/> MINT-84     | <input checked="" type="checkbox"/> MPIDB-0          | <input checked="" type="checkbox"/> Reactome-0      | <input checked="" type="checkbox"/> Reactome-Fls-29      |
| <input type="checkbox"/> Spike                  | <input type="checkbox"/> TopFind                     | <input checked="" type="checkbox"/> UniProt-25      | <input type="checkbox"/> VirHostNet                      |
| <input type="checkbox"/> ZINC                   |  |   |  |

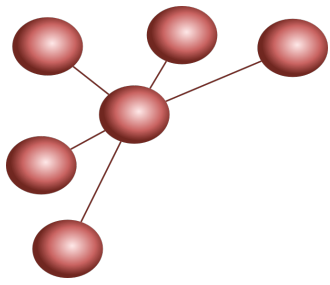
### Status of the service

- ONLINE
- OFFLINE
- WARNING: Time out
- ERROR: Unexpected Error

1,832 selected interactions

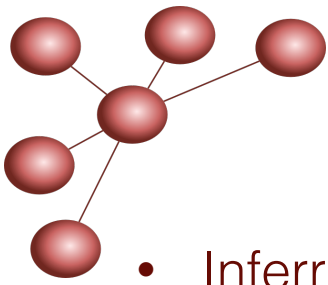
Cluster this query





# Part 1: Building Biological Networks

- From literature, knowledge, curation
- From large-scale interaction experiments
- **From inference from large-scale omics data**



# Network inference from -omics data

- Inferring/learning regulatory interactions from gene expression data (time-series, perturbation experiments)
- Famous methods: WGCNA, GENIE3
- Now on single-cells

Greenfield A, Madar A, Ostrer H, Bonneau R (2010) DREAM4: Combining Genetic and Dynamic Information to Identify Biological Networks and Dynamical Models. PLoS ONE 5(10): e13397.

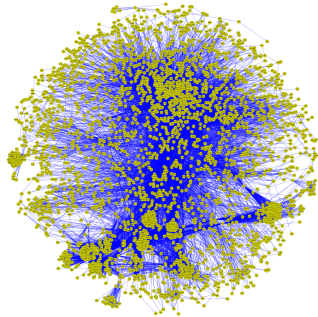
Saint-Antoine, M. M. & Singh, A. Network inference in systems biology: recent developments, challenges, and applications. *Current Opinion in Biotechnology* **63**, 89–98 (2020).

Algorithm Class	Temporal Data Required?	Directionality	Advantages	Disadvantages	Examples
Correlation	No	Undirected	<ul style="list-style-type: none"> <li>• Fast, scalable</li> <li>• Detection of feed-forward loops, fan-ins, and fan-outs</li> </ul>	<ul style="list-style-type: none"> <li>• Possibly over-simplistic</li> <li>• False positives for cascades</li> </ul>	WGCNA [13] PGCNA [14]
Regression	No	Directed	<ul style="list-style-type: none"> <li>• Good overall accuracy</li> </ul>	<ul style="list-style-type: none"> <li>• Bad detection of feed-forward loops, fan-ins, and fan-outs</li> </ul>	TIGRESS [15], GENIE3 [16], bLARS [17]
Bayesian - Simple	No	Directed	<ul style="list-style-type: none"> <li>• Performance on small networks</li> </ul>	<ul style="list-style-type: none"> <li>• Performance on large networks.</li> <li>• Inability to detect cycles</li> </ul>	[19,20]
Bayesian - Dynamic	Yes	Directed	<ul style="list-style-type: none"> <li>• Performance on small networks</li> <li>• Detection of cycles and self-edges</li> </ul>	<ul style="list-style-type: none"> <li>• Performance on large networks.</li> </ul>	[21]
Information Theory	No	Undirected (at least in simplest form)	<ul style="list-style-type: none"> <li>• Detection of feed-forward loops, fan-ins, and fan-outs</li> <li>• Similar to correlation methods, with better accuracy</li> </ul>	<ul style="list-style-type: none"> <li>• False positives for cascades</li> </ul>	ARACNE [25], CLR [26], MRNET [27], PIDC [28]
Phixer	No	Directed	<ul style="list-style-type: none"> <li>• Parsimonious output due to pruning step.</li> </ul>	<ul style="list-style-type: none"> <li>• Possible loss of overall accuracy due to pruning step (this can be removed if the user chooses)</li> </ul>	[31]

# Interactome(s)



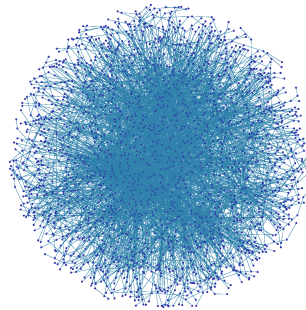
**Pathways**



~250 000 edges

Curated  
networks

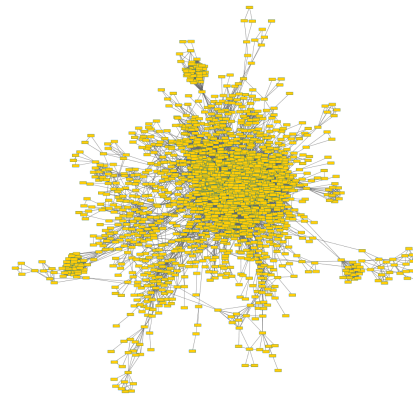
**PPI**



~60 000 edges

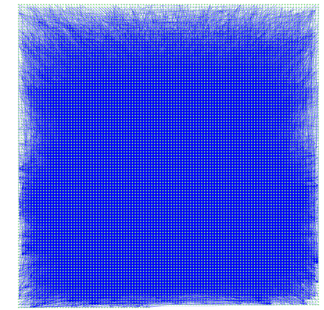
Measured  
networks

**Complexes**



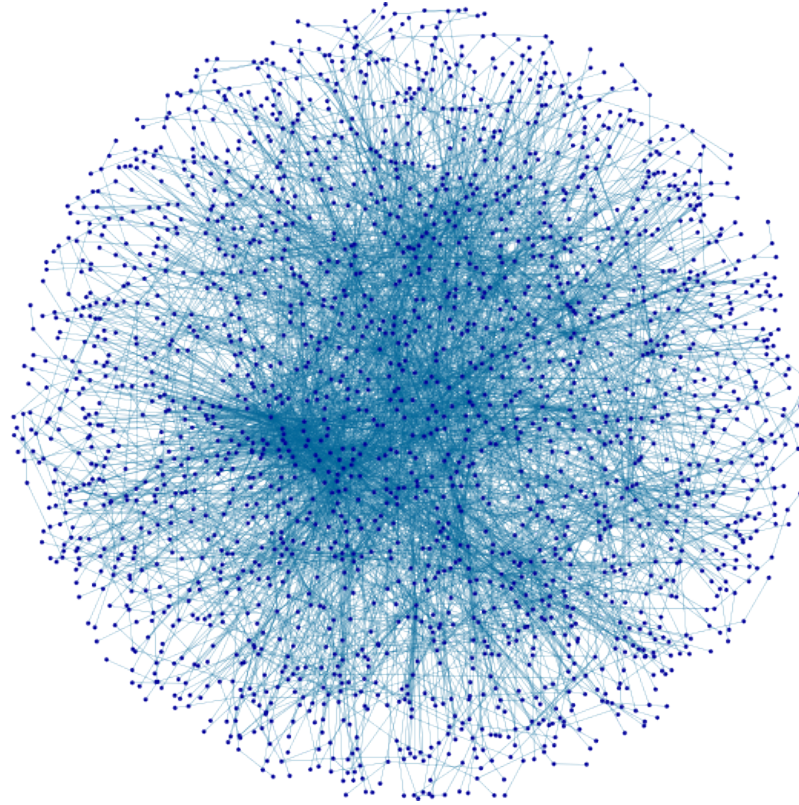
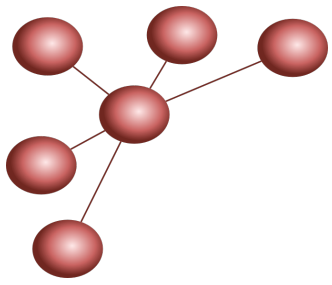
~40 000 edges

**Correlation of  
expression**



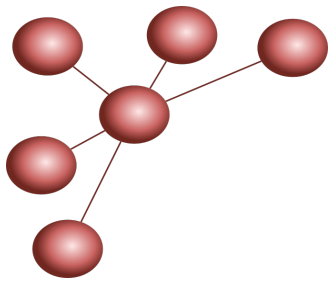
~1 400 000 edges

Inferred  
networks

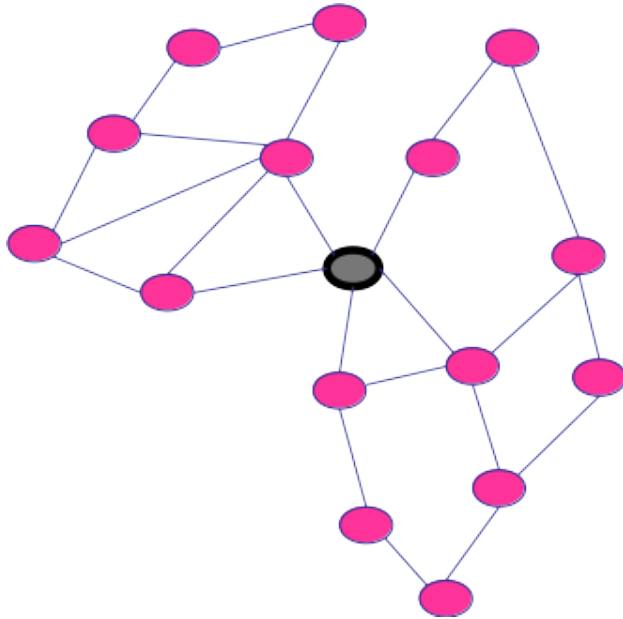


**Part2: What's next ?  
=> Network Analysis**

**Network metrics / Network algorithms**



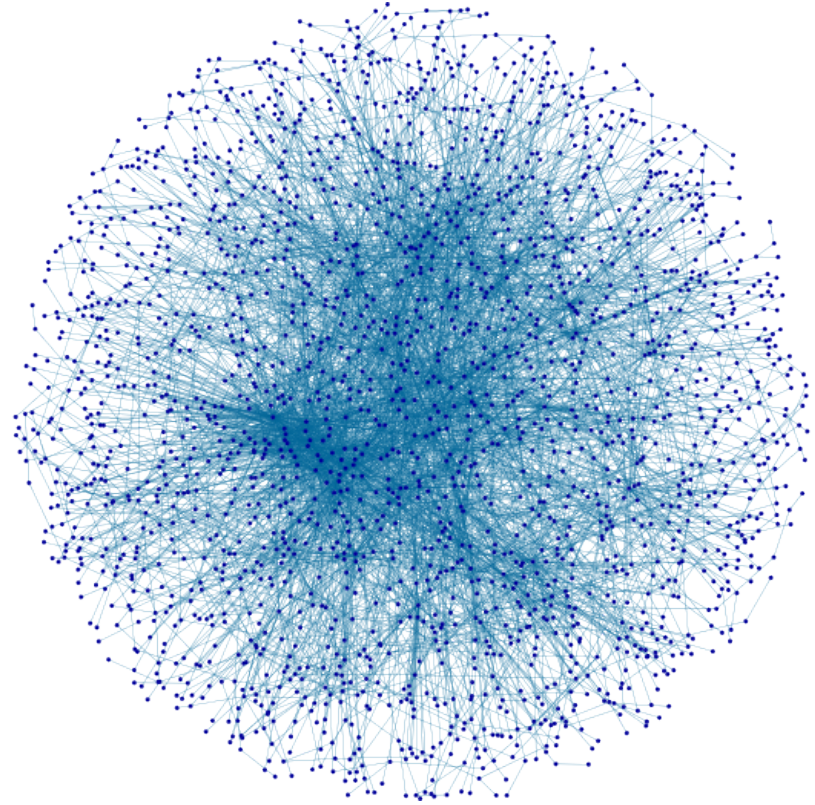
**Local approaches**



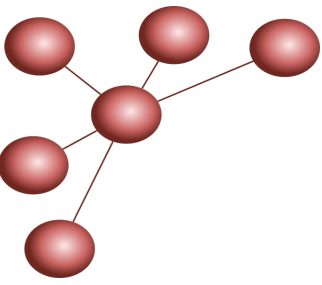
- **mathematical modelling**
- **“guilt by association”**

# How to use large-scale biological networks ?

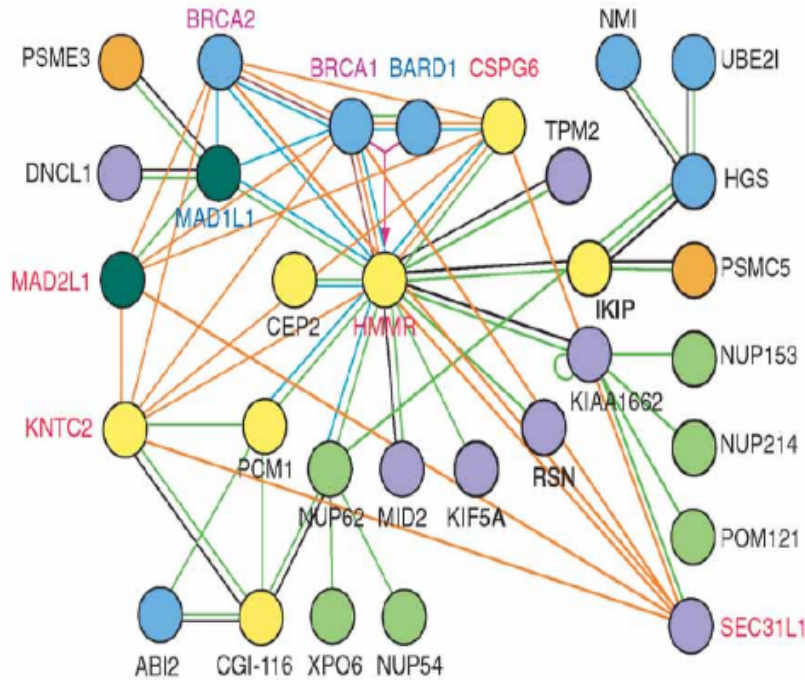
**Global approaches**



- **Topological features**
- **Network analysis algorithms**



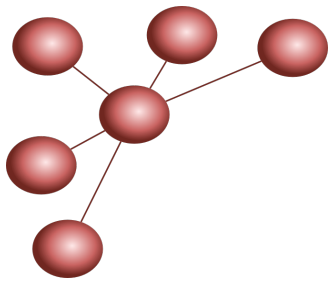
# Local approach: identification of a new gene involved in breast cancer



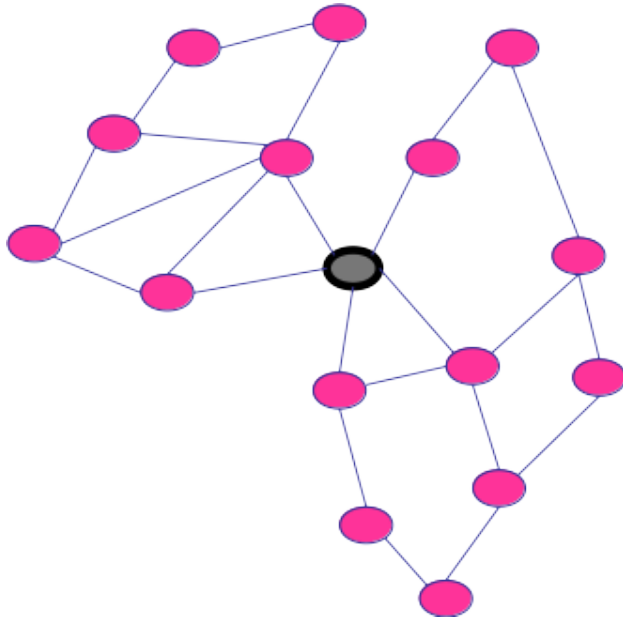
**Nodes correspond to proteins,  
edges to interactions identified  
by different experimental  
techniques**

## Functional associations (*n*)

- Expression profiling similarity (20)
- Similar gene deficiency phenotype (2)
- Y2H binary protein interaction (32)
- Protein co-AP (13)
- Protein co-IP (11)
- Biochemical interaction (1)



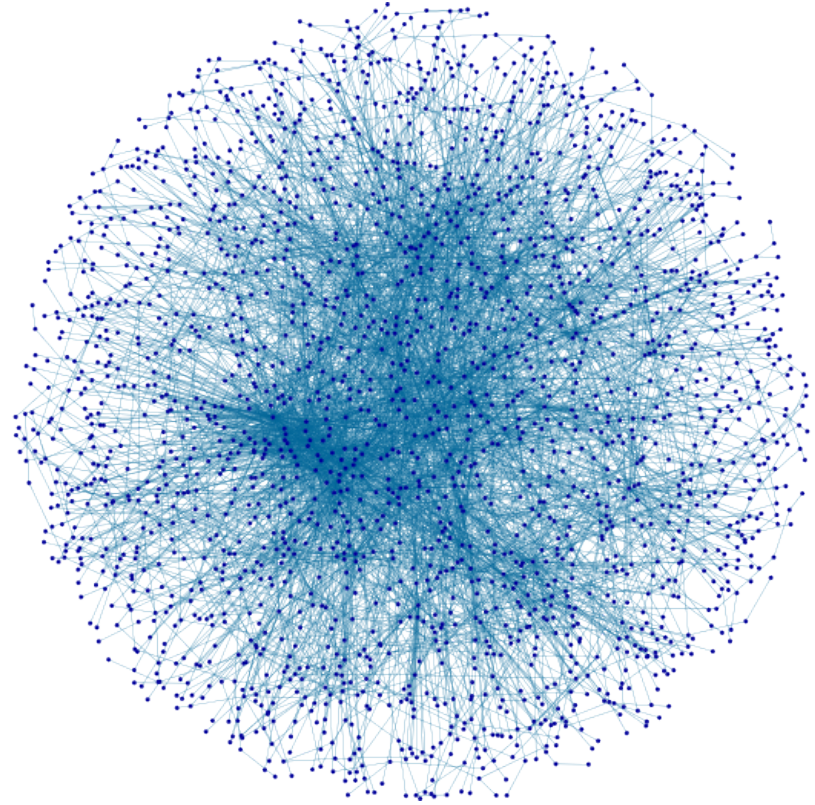
**Local approaches**



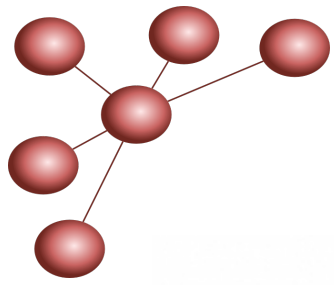
- **mathematical modelling**
- **“guilt by association”**

# How to use large-scale biological networks ?

**Global approaches**

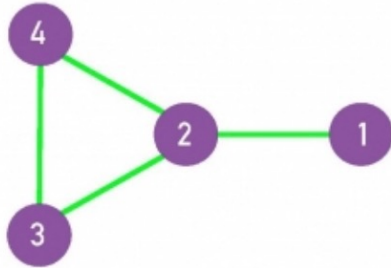


- **Topological features**
- **Network analysis algorithms**

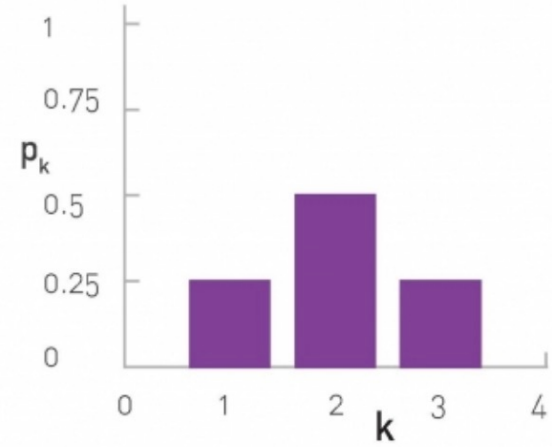


# Degree distribution

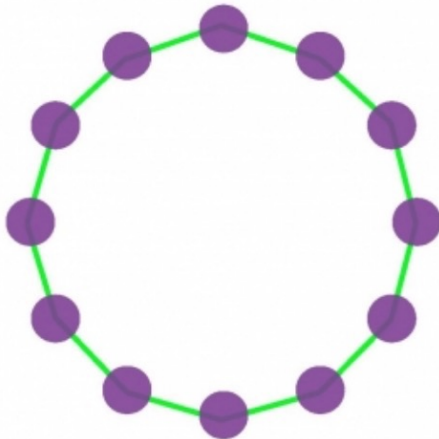
a.



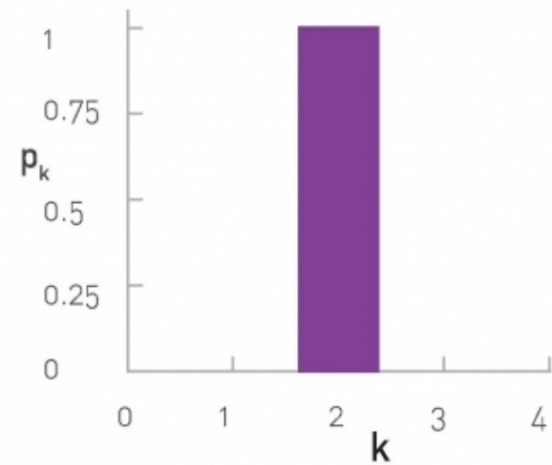
b.



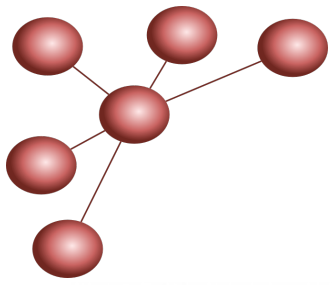
c.



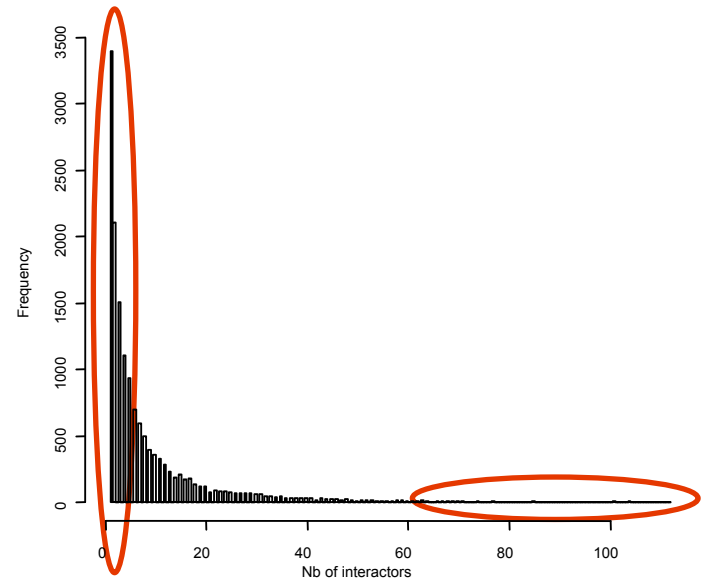
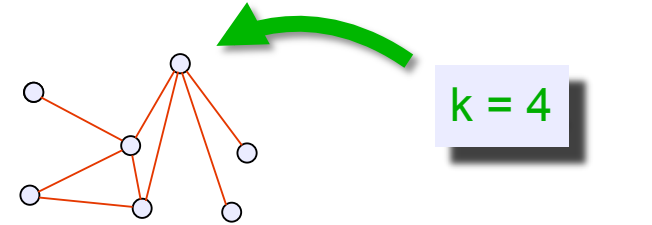
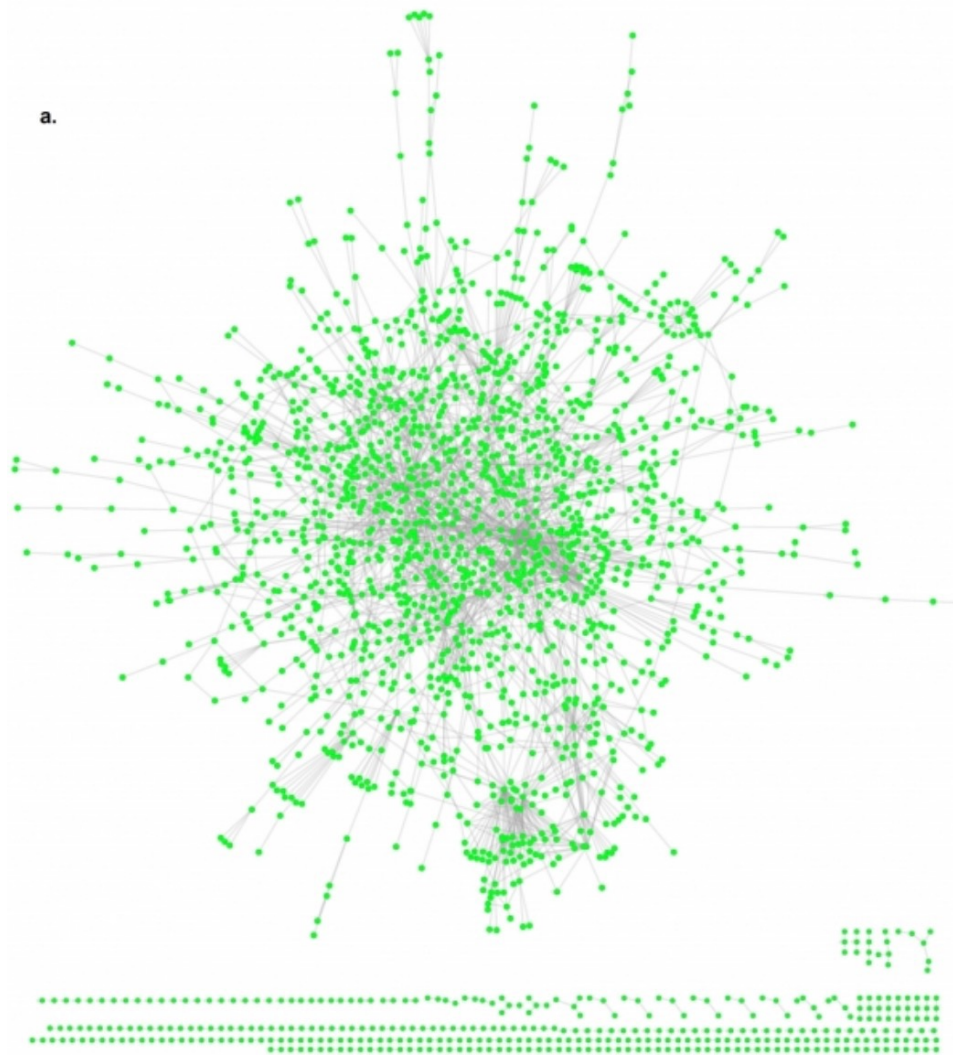
d.



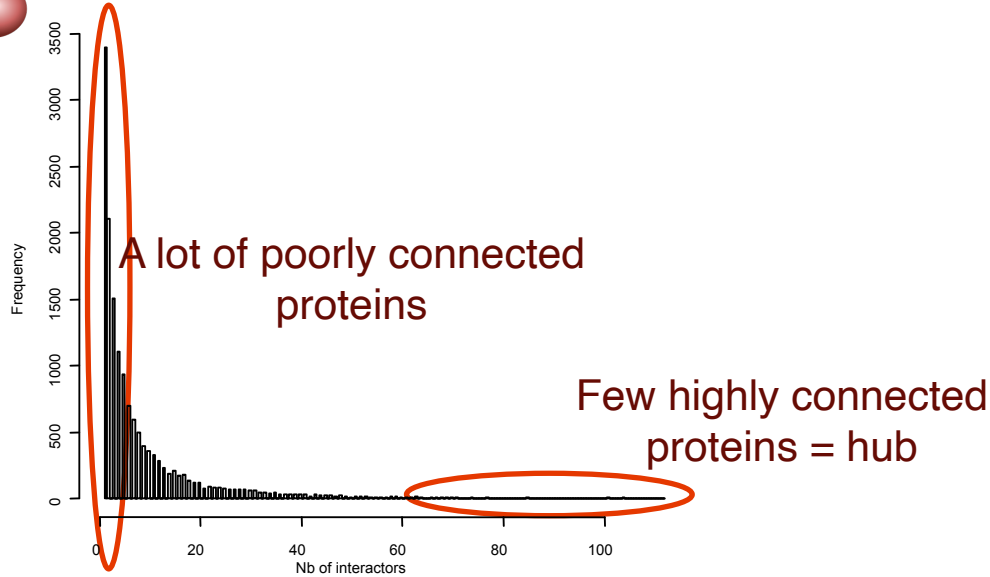
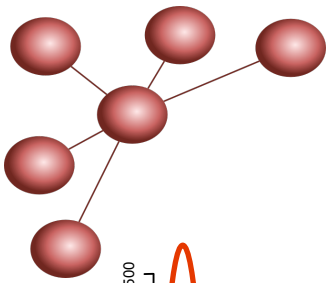




# Degree distribution

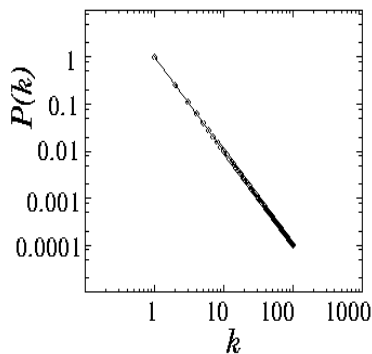


# Protein degree distribution : interactomes are scale-free and small-world



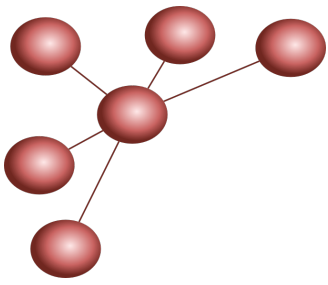
Scale-free

Power-law distribution

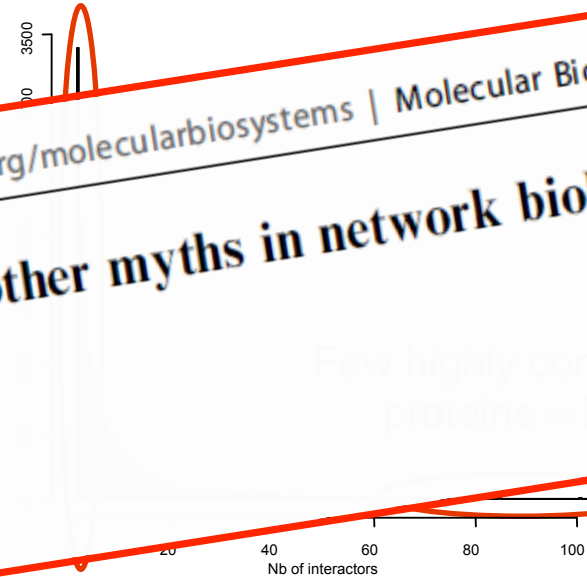


Biological interpretation?

- Growth with preferential attachment (“rich get richer”) => create “hubs”
- Robust to random attack, sensitive to targeted attacks



# Protein degree distribution : interactomes are scale-free and small-world



www.rsc.org/molecularbiosystems | Molecular BioSystems

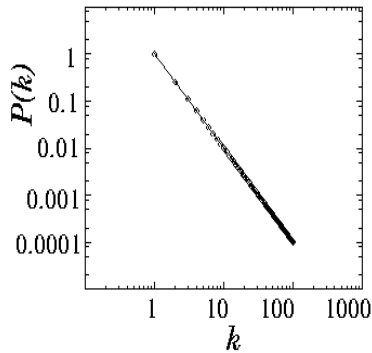
REVIEW

## The powerful law of the power law and other myths in network biology†

Gipsi Lima-Mendez\* and Jacques van Helden\*

Received 5th May 2009, Accepted 12th August 2009  
 First published as an Advance Article on the web  
 DOI: 10.1039/b908681a

A lot of poorly connected proteins



power-law distribution

ARTICLE

<https://doi.org/10.1038/s41467-019-08746-5> OPEN

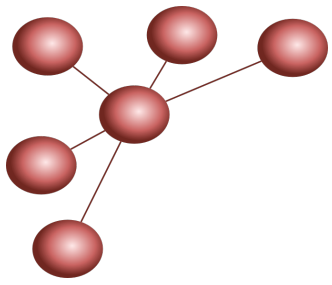
## Scale-free networks are rare

Anna D. Broido<sup>1</sup> & Aaron Clauset<sup>2,3,4</sup>

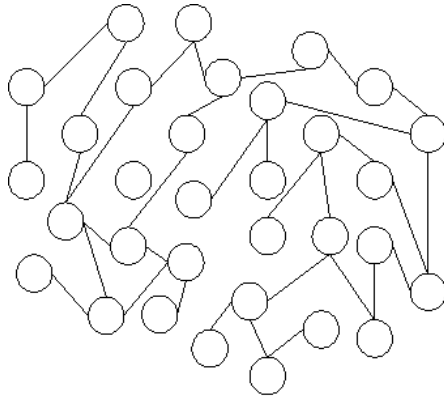
targetted

rich-get-richer attachment ("rich get richer")

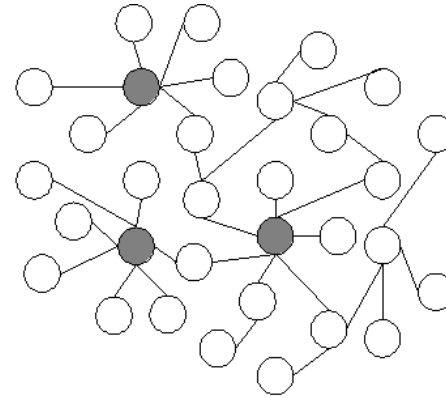
→ create "hubs"



# Network topological structure : Small-world property



(a) Random network



(b) Scale-free network

- Milgram, 6 degrees of separation

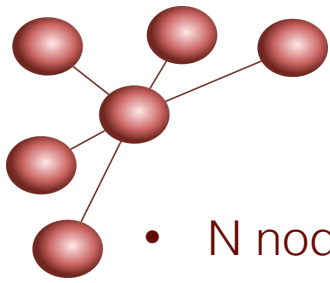
SIX DEGREES OF  
**WIKIPEDIA**

About | Blog | GitHub

Find the shortest paths from

Nibiru cataclysm to Delta Air Lines

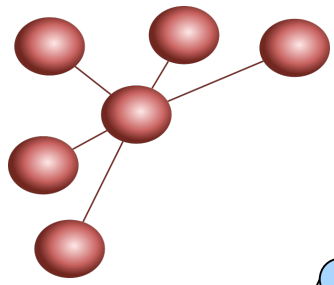
Go!



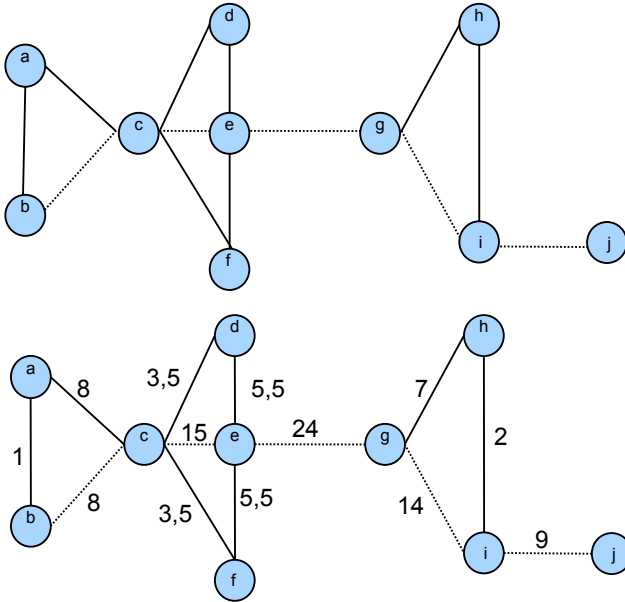
# Metrics on graphs

- N nodes, V edges
- Network size
- Adjacency matrix
- Degree, degree distribution
- Path, shortest path, distances
- Connectivity, clustering coefficient
- Betweenness
- Motifs

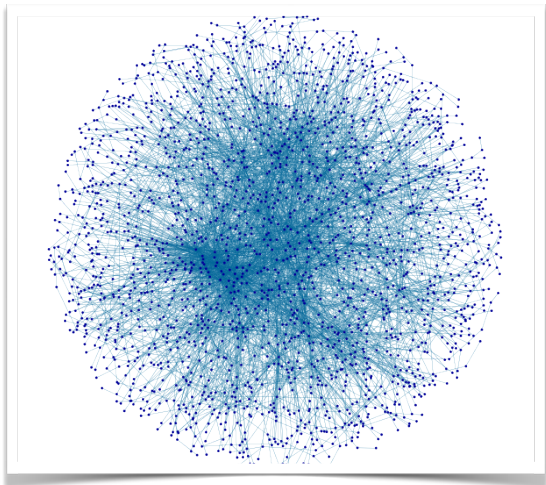
NETWORK MEASURES				
Degree/ connectivity (k)	Clustering coefficient/ interconnectivity (C)	Assortativity/average nearest neighbor's connectivity (NC)	Shortest path (SP) between two nodes	Betweenness/ centrality (B)
<p><math>k_A = \text{Nb of edges through } A = 5</math></p>	$C_A = \frac{\text{Actual links between A's neighbors (black)}}{\text{Possible links between A's neighbors (orange)}}$ $C_A = n_A / [k_A(k_A - 1) / 2]$ $= 2 / [4 \times (4 - 1) / 2] = 0.333$	$NC_A = (k_B + k_C + k_D + k_E + k_J) / 5$ $= (5 + 2 + 2 + 3 + 1) / 5 = 2.6$	<p><math>SP_{FH} = (F, D, A, B, H) = 4</math></p>	<p><math>B_4 = \text{Fraction of SPs passing through } A = 0.090</math></p>

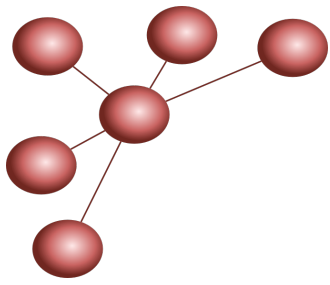


# “Edge Betweenness”



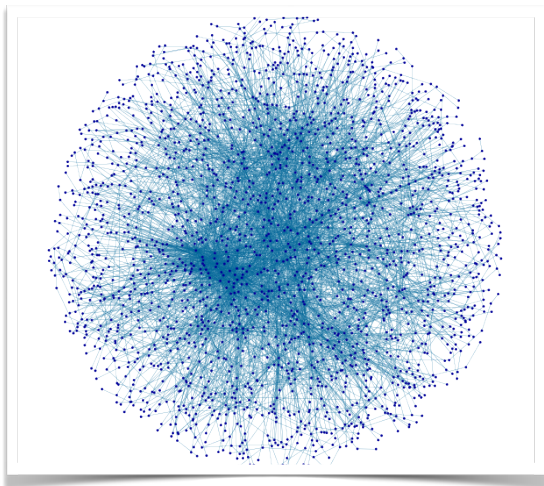
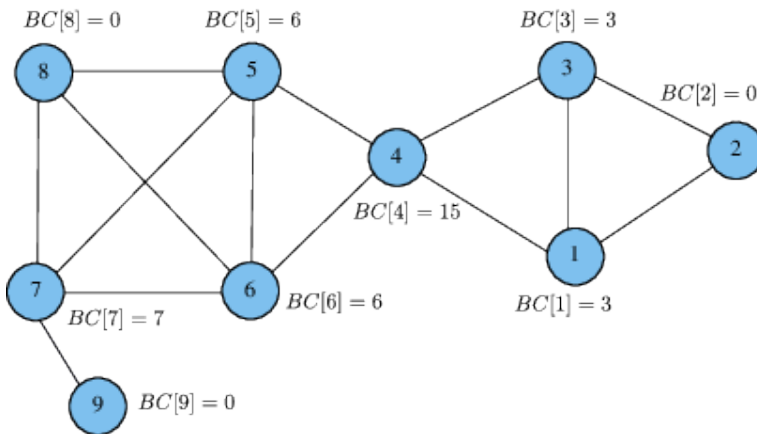
Number of shortest paths  
running through an edge  
=  
“bottleneck”



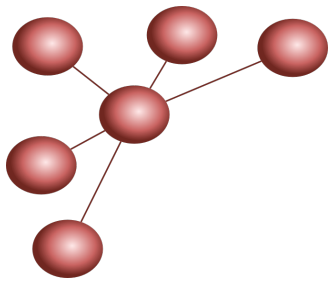


# “Node Betweenness”

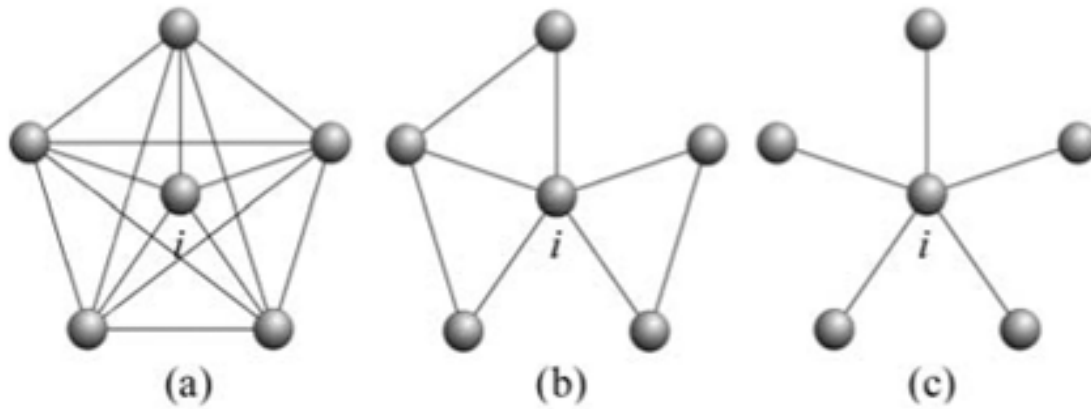
Number of shortest paths  
running through a node  
=  
“bottleneck”



Biological interpretation ?  
Correlation with gene essentiality, gene  
involvement in diseases, importance in  
flux transmission ...

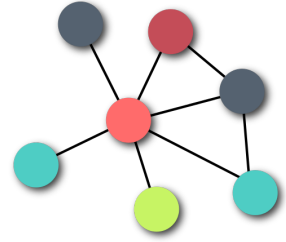


# Clustering coefficient / modularity



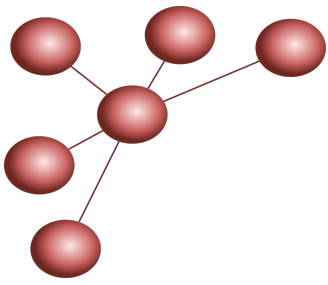
**Actual links between neighbours / Possible links between neighbours**



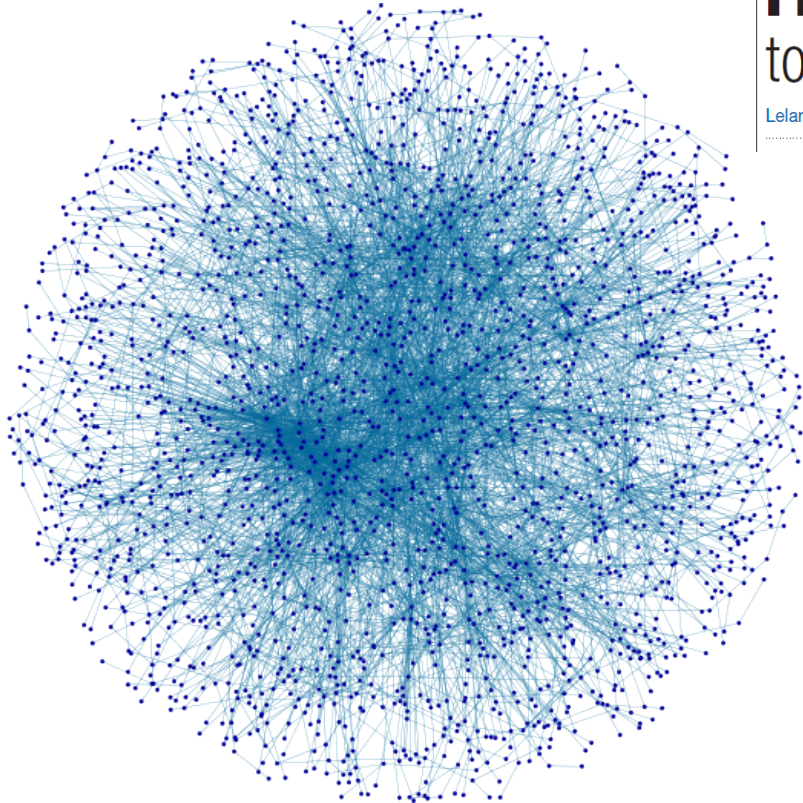


# Algorithms for Network Analysis

- Clustering
- Exploration with Random Walk with Restart
- Integration of expression data to find active modules



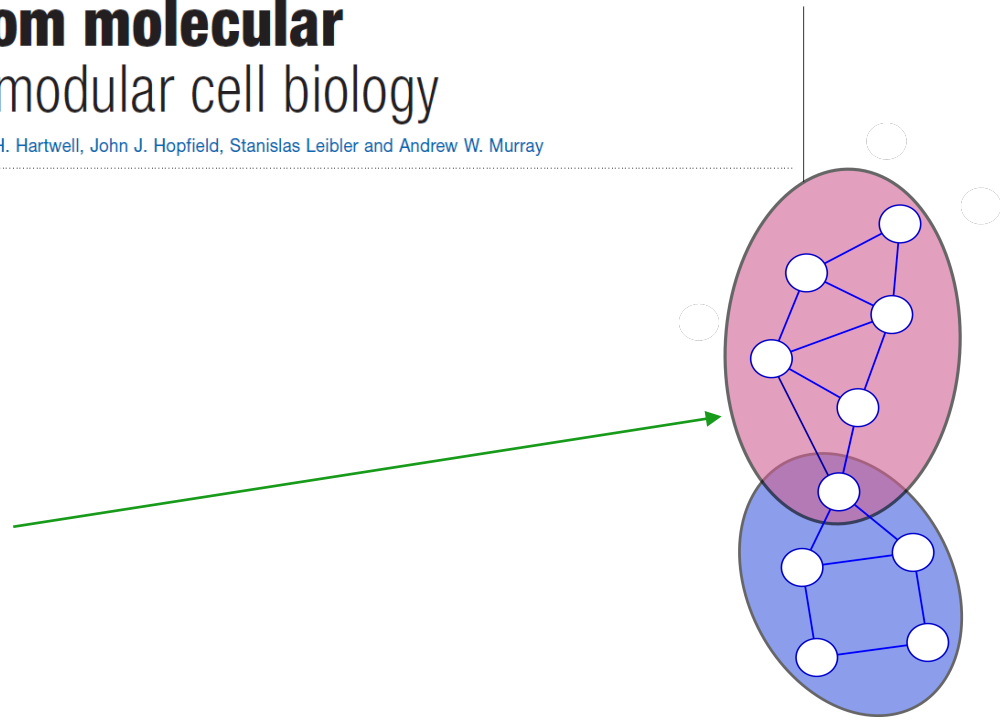
# Network Analysis - Clustering



**From molecular**  
to modular cell biology

Leland H. Hartwell, John J. Hopfield, Stanislas Leibler and Andrew W. Murray

impacts



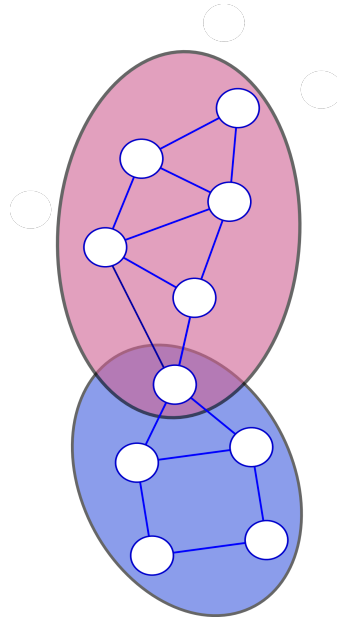
**Functional module / community / cluster / class : discrete function**

**Modules can be isolated or connected**

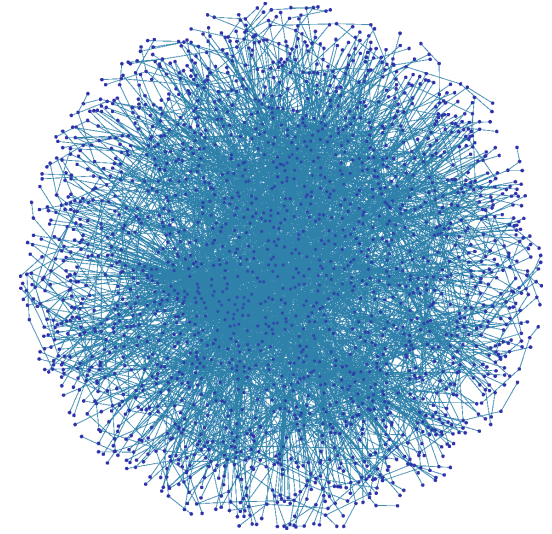
**Groups of proteins involved in a common cellular function**



**Binary interaction**



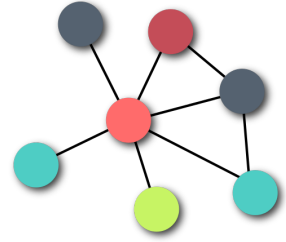
**Functional modules**



**Interaction Networks**

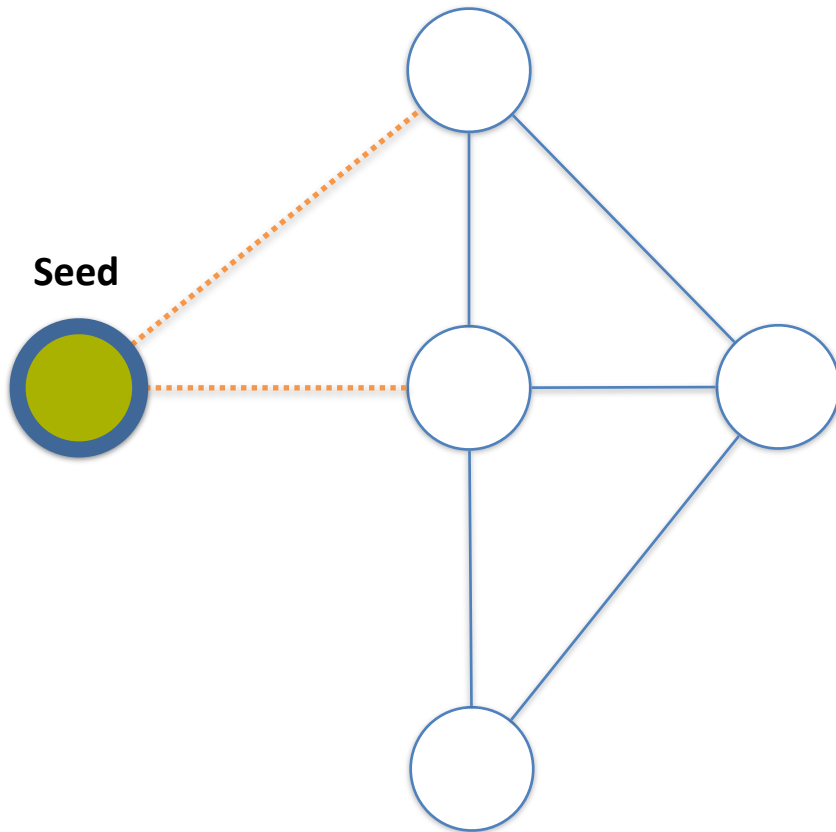
**Precision**

**Comprehensiveness**

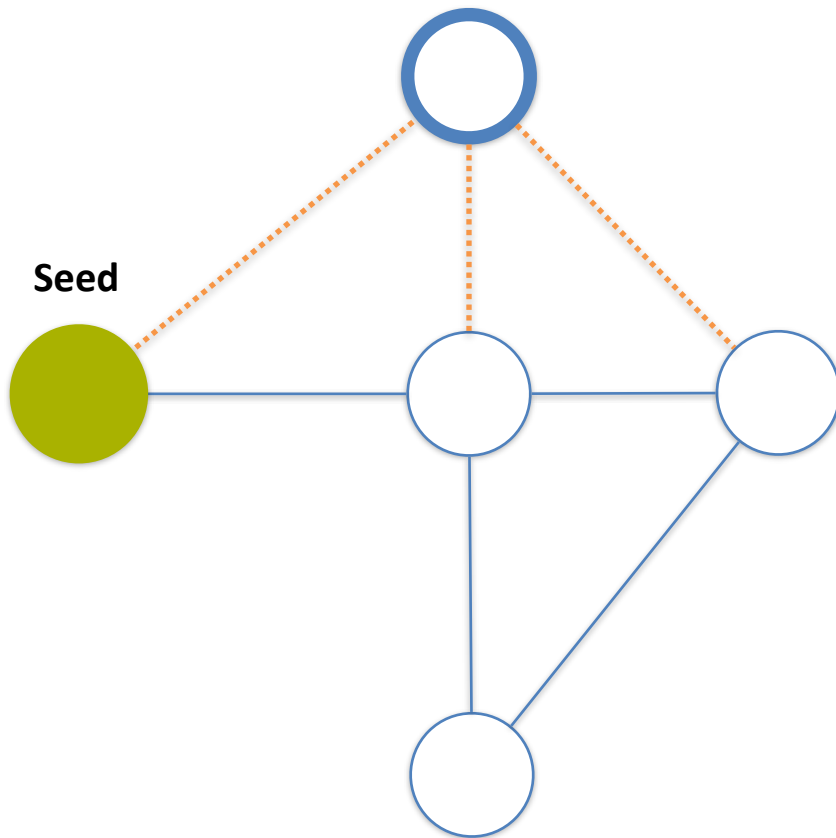


# Network Exploration: Random Walk with Restart

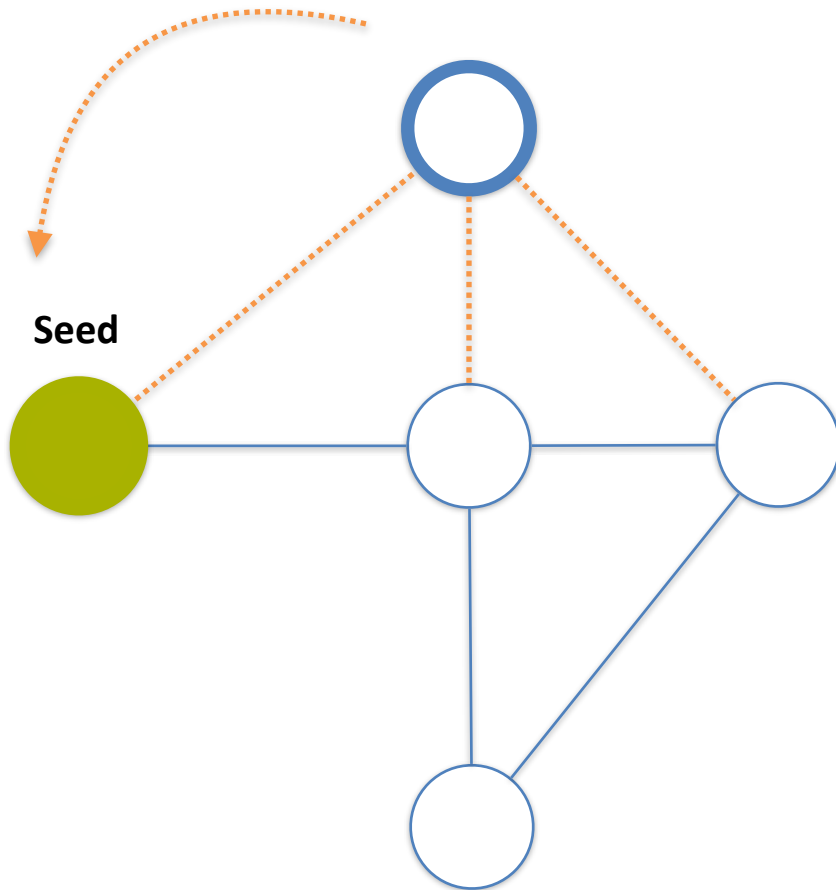
# The Random Walk with Restart algorithm



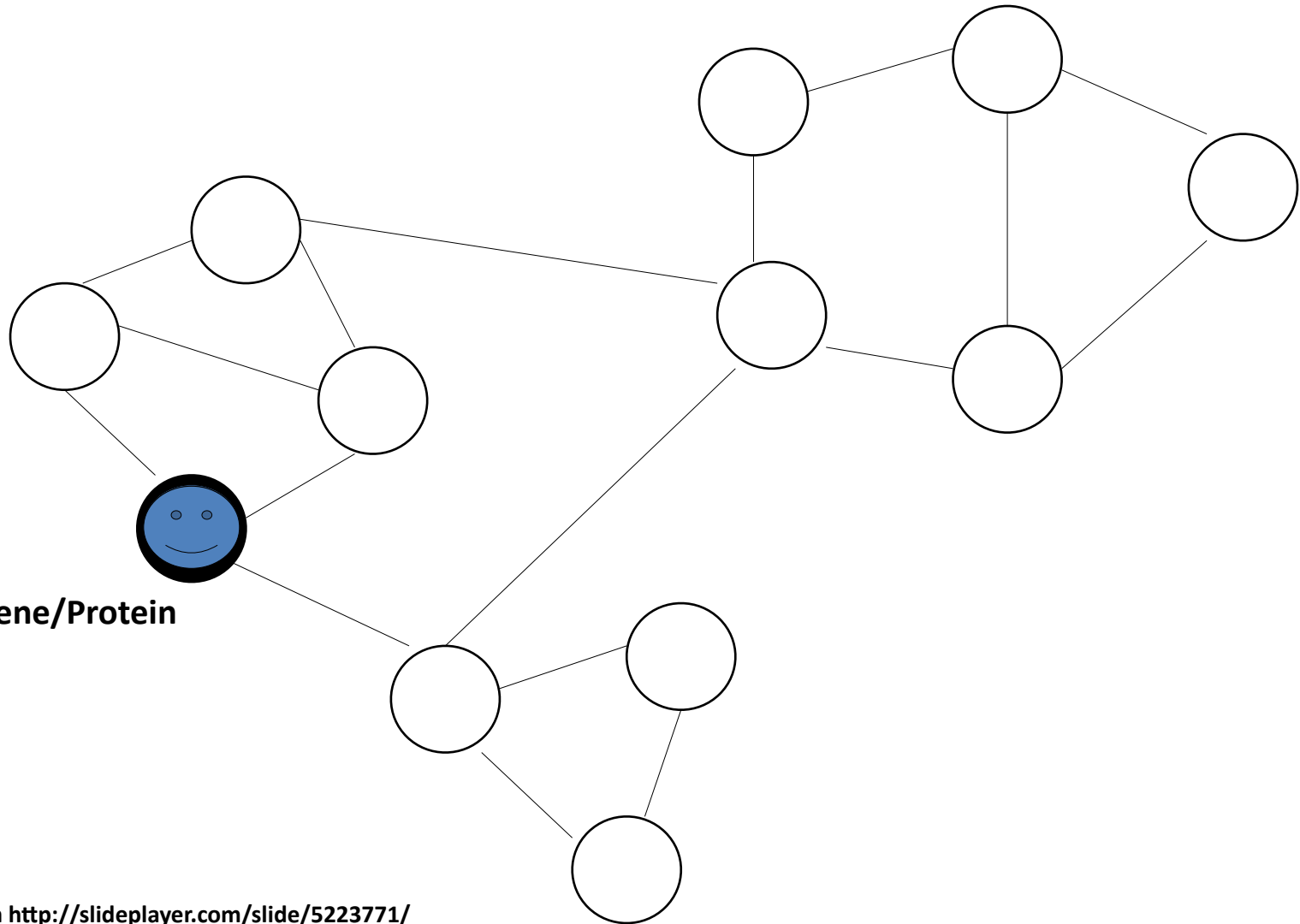
# The Random Walk with Restart algorithm



# The Random Walk with Restart algorithm

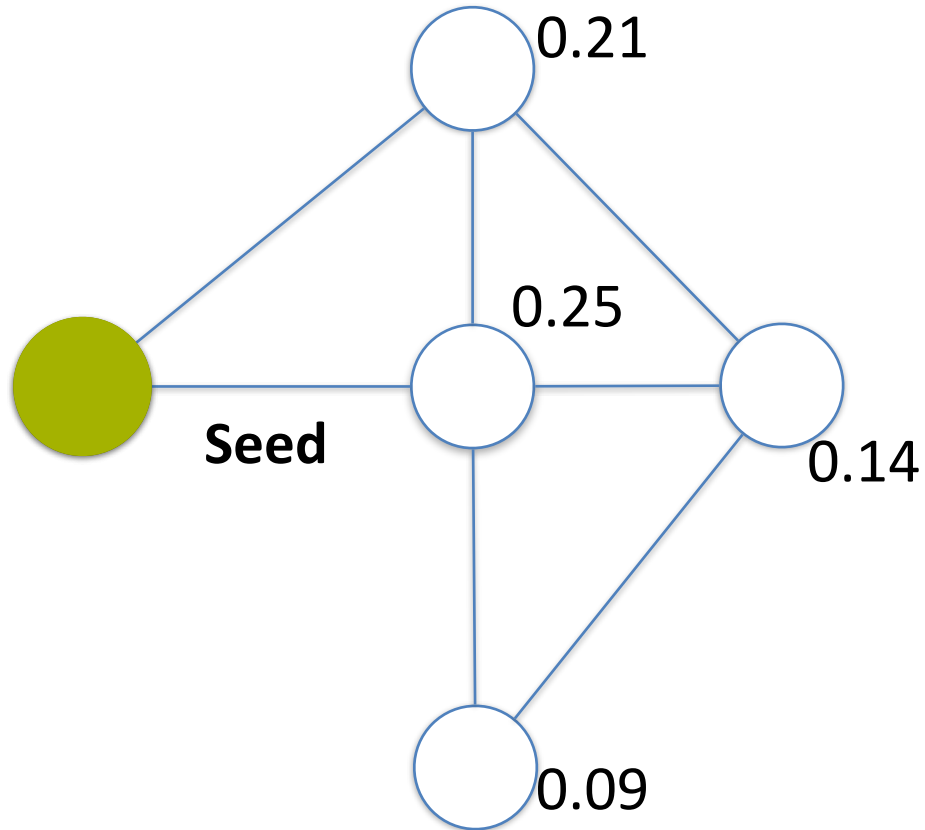


# The Random Walk with Restart algorithm

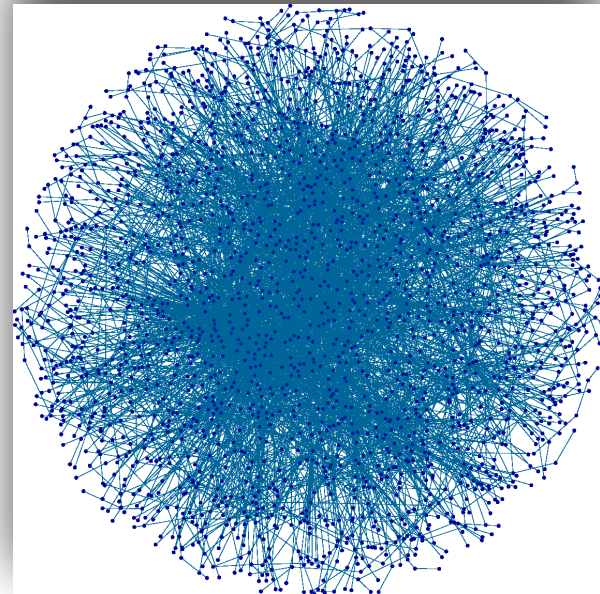




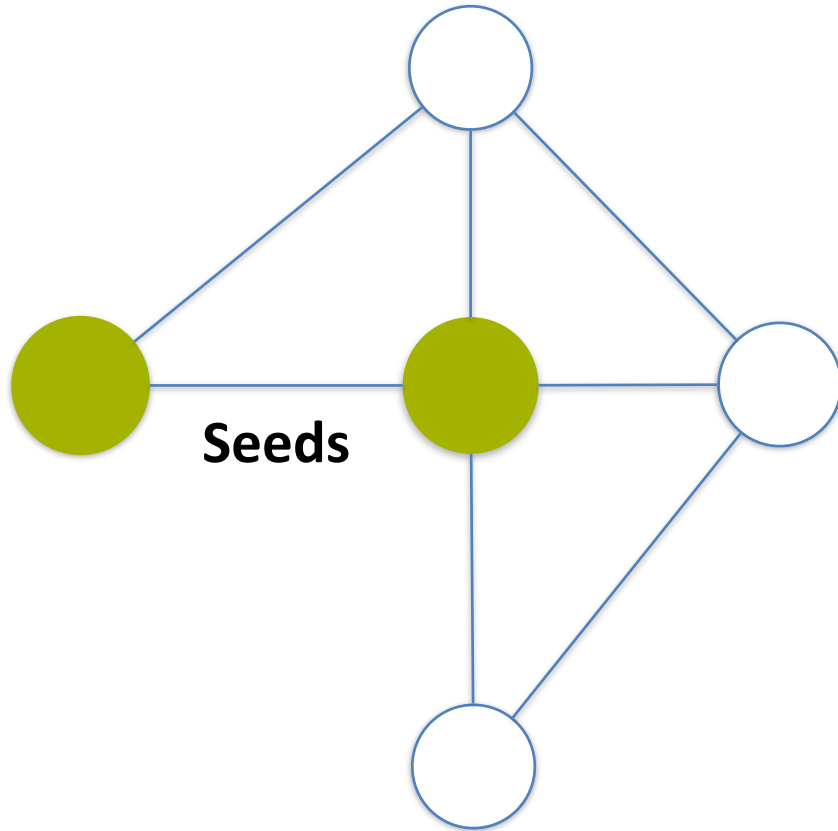
# The Random Walk with Restart algorithm



- Local exploration
- Proximity/pertinence score *wrt* the seed

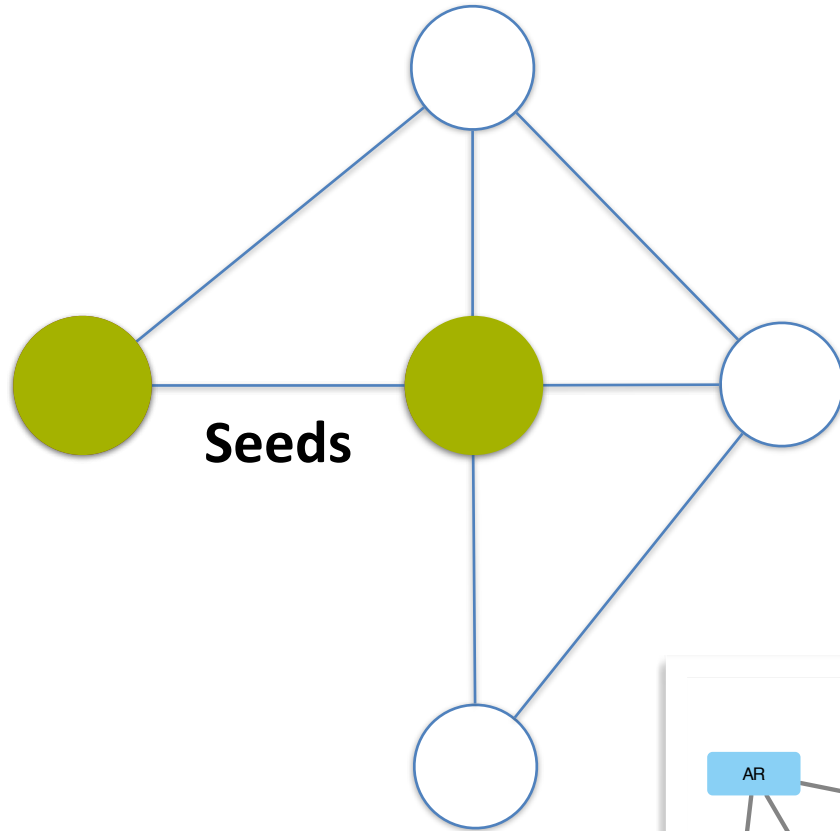


# The Random Walk with Restart algorithm

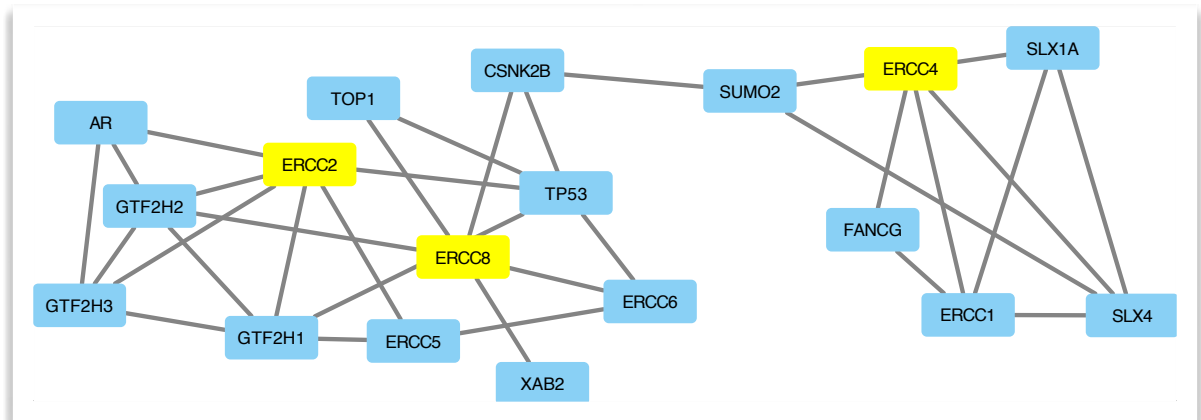


- Local exploration
- Proximity/pertinence score *wrt* the seed(s)

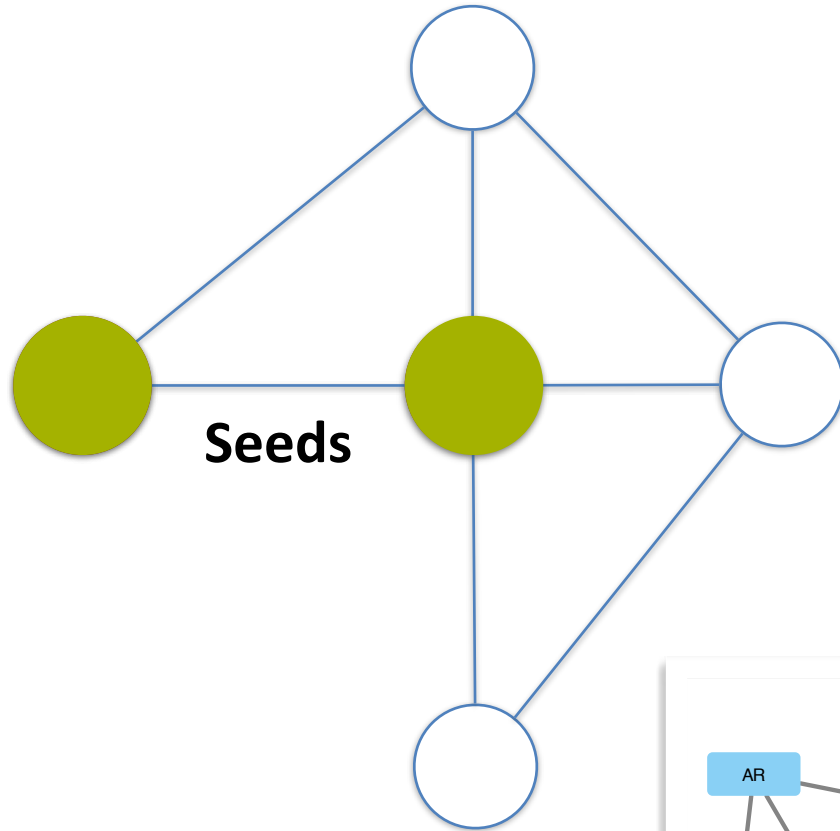
# The Random Walk with Restart algorithm



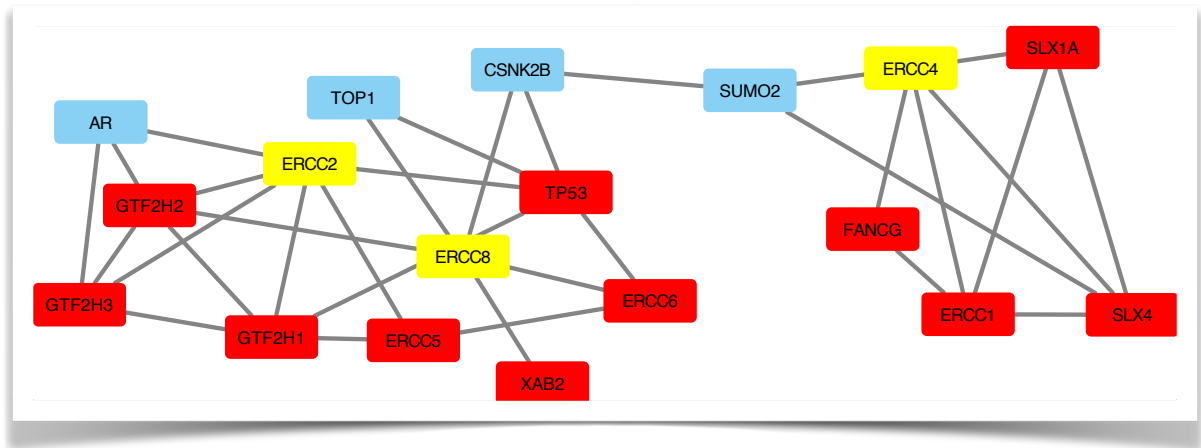
- Local exploration
- Proximity/pertinence score *wrt* the seed(s)
- Guilt-by association



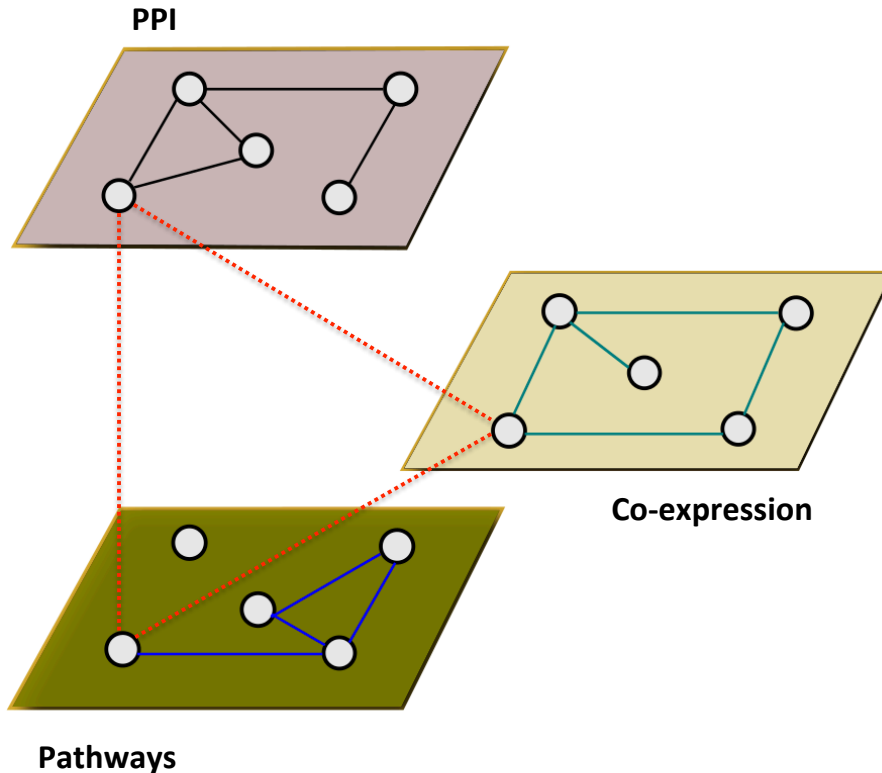
# The Random Walk with Restart algorithm



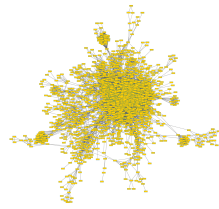
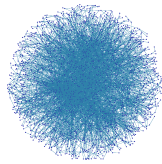
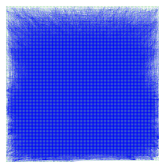
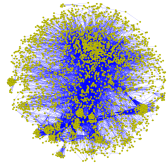
- Local exploration
- Proximity/pertinence score *wrt* the seed(s)
- Guilt-by association



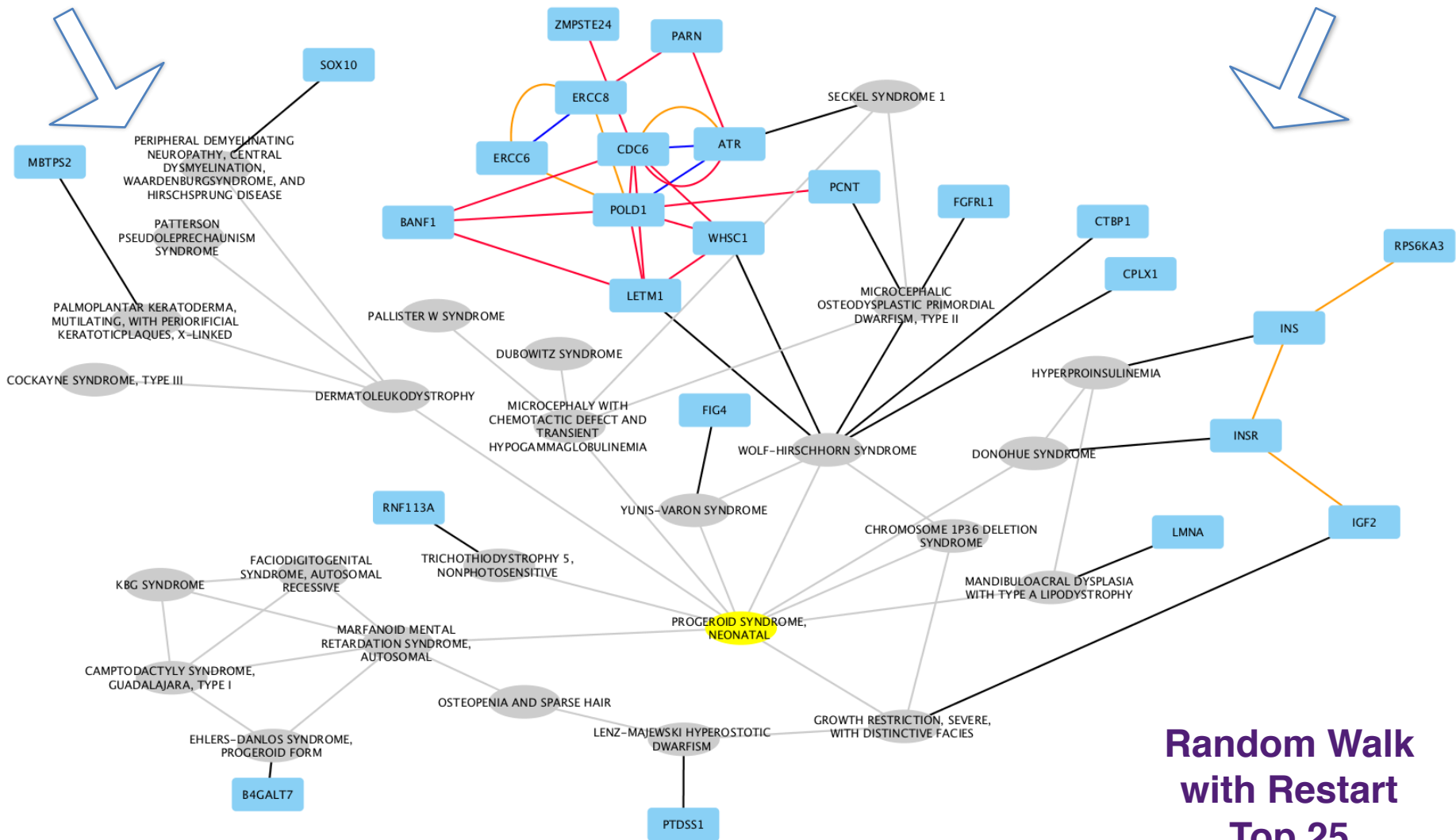
# Random Walk with Restart on Multiplex Networks (RWR-M)



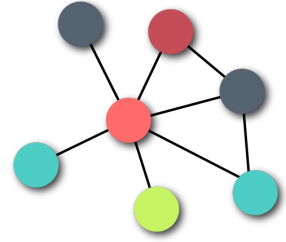
- Walk one layer
- Jump across layers
- Gene/Protein Seed(s)



# Disease-disease network



Random Walk with Restart  
Top 25



# Integrating expression data and networks: finding active modules

Interactomes are devoid of spatio-temporal information

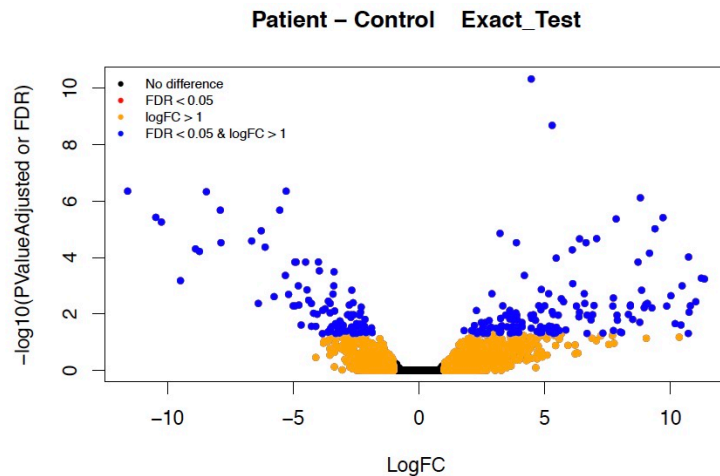
# RNA-seq transcriptomics analyses



RNA-seq transcriptomics data



Identify significant DE mRNAs



Functional enrichments



# Active module identification



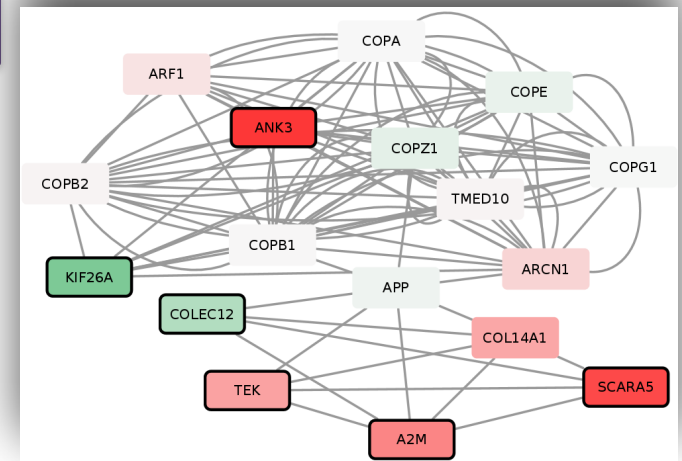
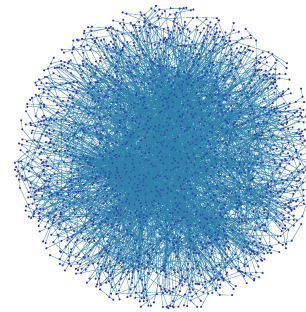
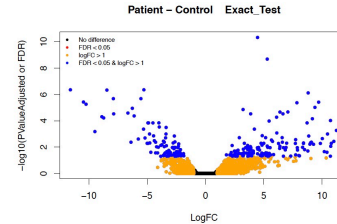
RNA-seq transcriptomics data

+

Biological Network



Find “active” subnetworks



Algorithms: Greedy searches (PinnacleZ), Simulated Annealing (jActiveModules), Genetic Algorithms (COSINE) (Ideker et al. 2002, Chuang et al. 2007, Ma et al. 2011, Ozisik et al. 2017...)

# Active module identification

---



- Few methods consider the density of interactions
- Methods are using only one (usually protein-protein) interaction networks

=> We propose a **Multi-Objective Genetic Algorithm** to identify active modules from Multiplex Networks

# 2 objectives to maximize



1

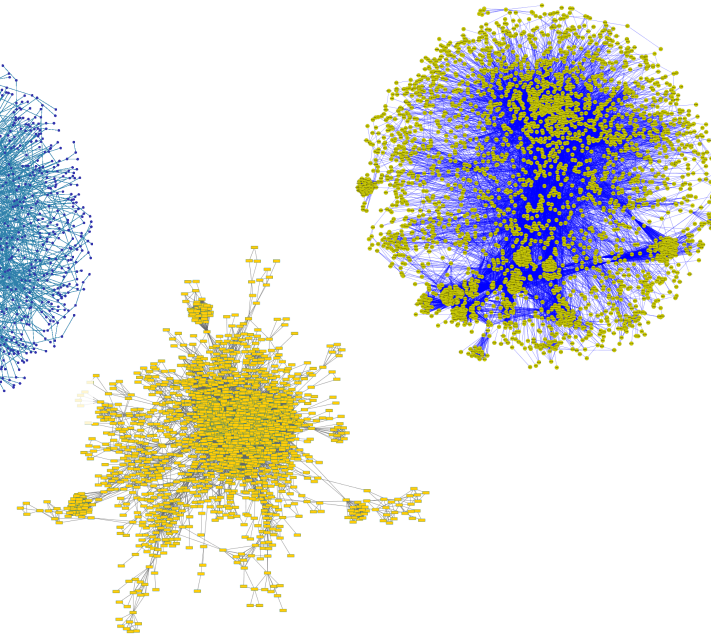
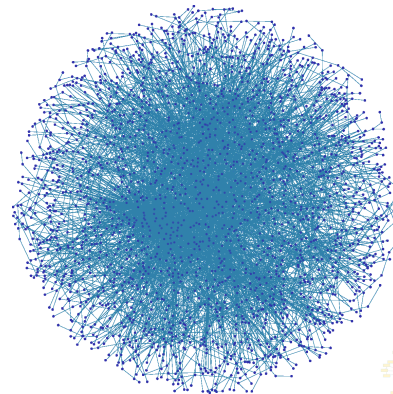
Average nodes score  $\overline{NodesScore} = \frac{1}{n} \sum_{i=1}^n (Score_i^{norm})$

$$Score_i^{norm} = \frac{Score_i - \min(Score)}{\max(Score) - \min(Score)} \quad Score_i = \Phi^{-1}(1 - p_i)$$

2

Density

$$D_{norm} = \sum_{l=1}^L \frac{d_s}{d_l}$$



# 2 objectives to maximize



1

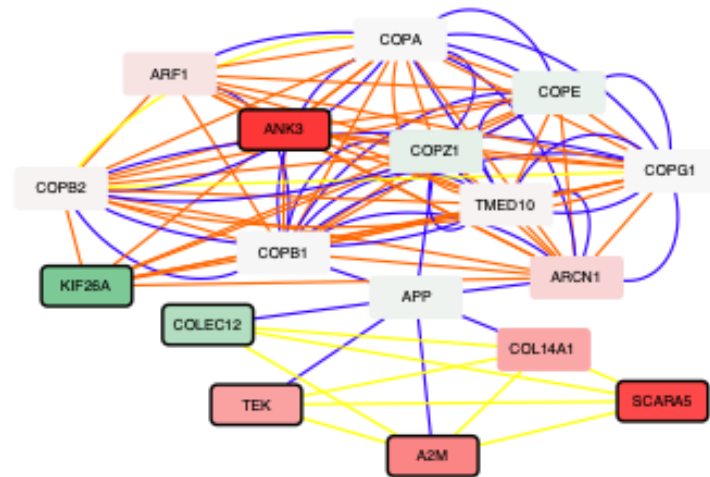
Average nodes score  $\overline{NodesScore} = \frac{1}{n} \sum_{i=1}^n (Score_i^{norm})$

$$Score_i^{norm} = \frac{Score_i - \min(Score)}{\max(Score) - \min(Score)} \quad Score_i = \Phi^{-1}(1 - p_i)$$

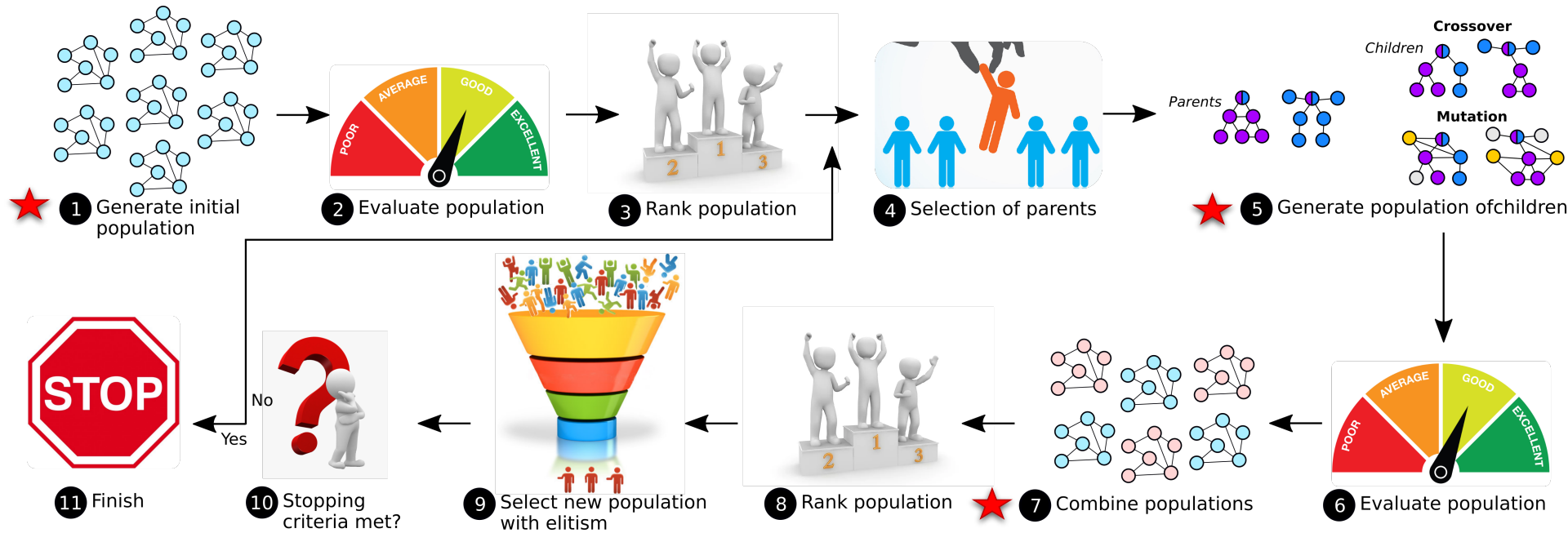
2

Density

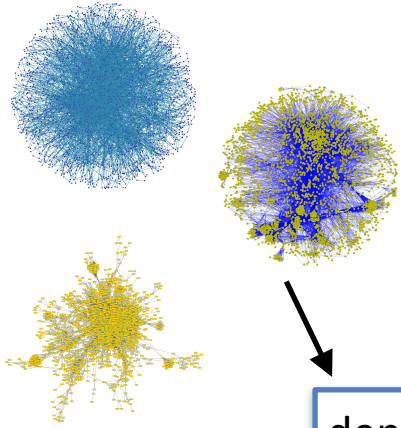
$$D_{norm} = \sum_{l=1}^L \frac{d_s}{d_l}$$



# Multi-Objectives Genetic Algorithm

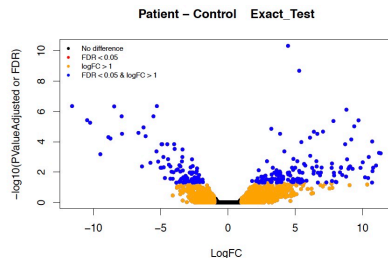
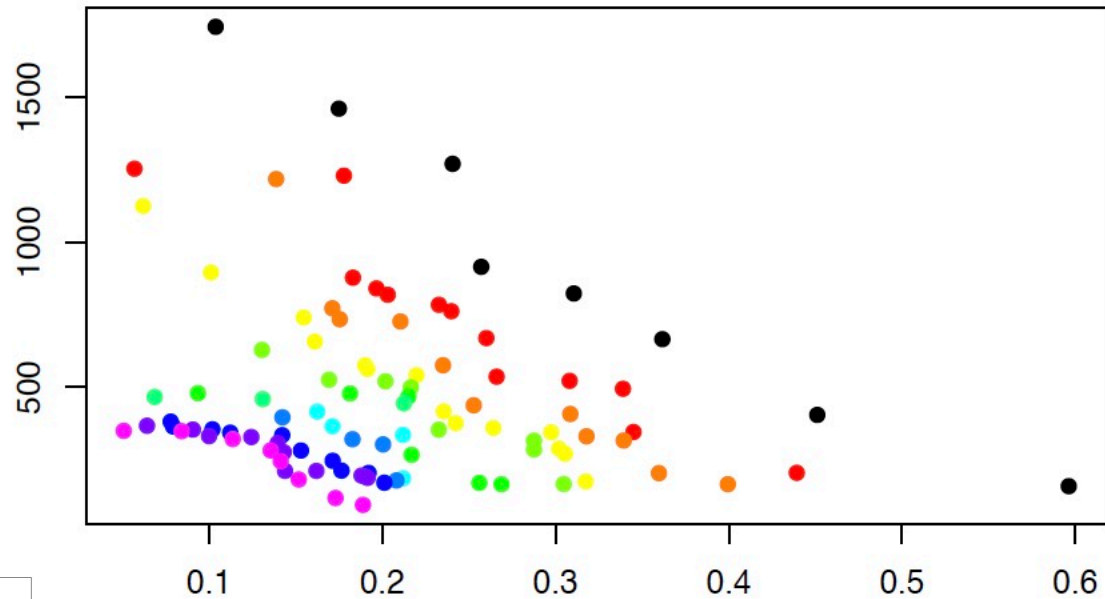


# Multi-objective Genetic Algorithm to find Active Modules in Multiplex Biological Networks



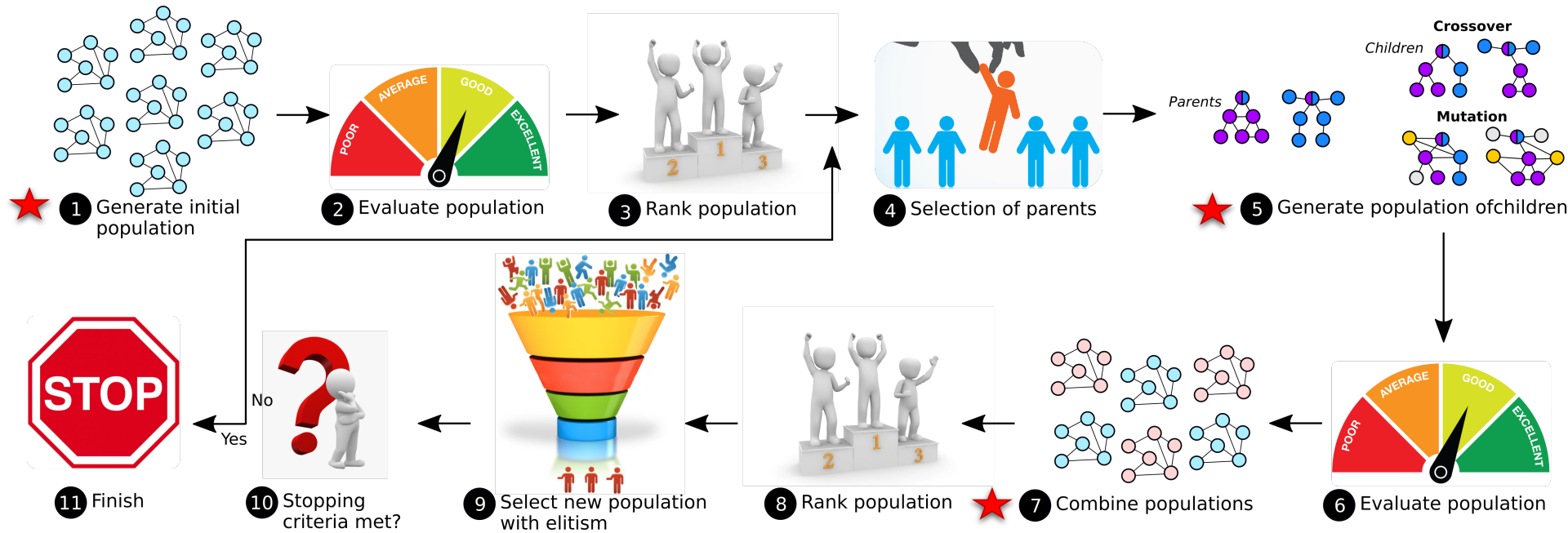
density of interactions from the multiplex network

Maximize 2 objectives



Differential expression (average node-scores)

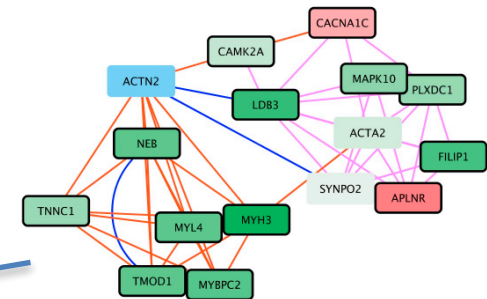
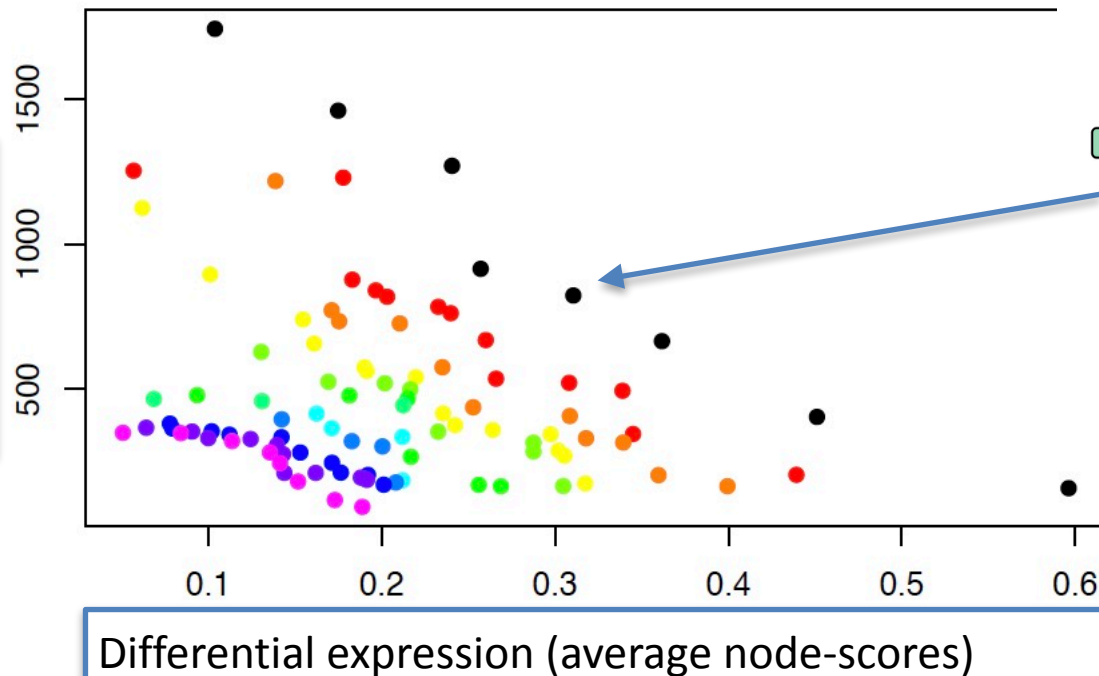
# Multi-Objectives Genetic Algorithm



# Multi-objective Genetic Algorithm to find Active Modules in Multiplex Biological Networks



## MOGAMUN



Novoa et al. BioRxiv, 2020  
Bioconductor

<https://github.com/elvanov/MOGAMUN>